

Testing LCDM with LISA

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Λ CDM

H_0

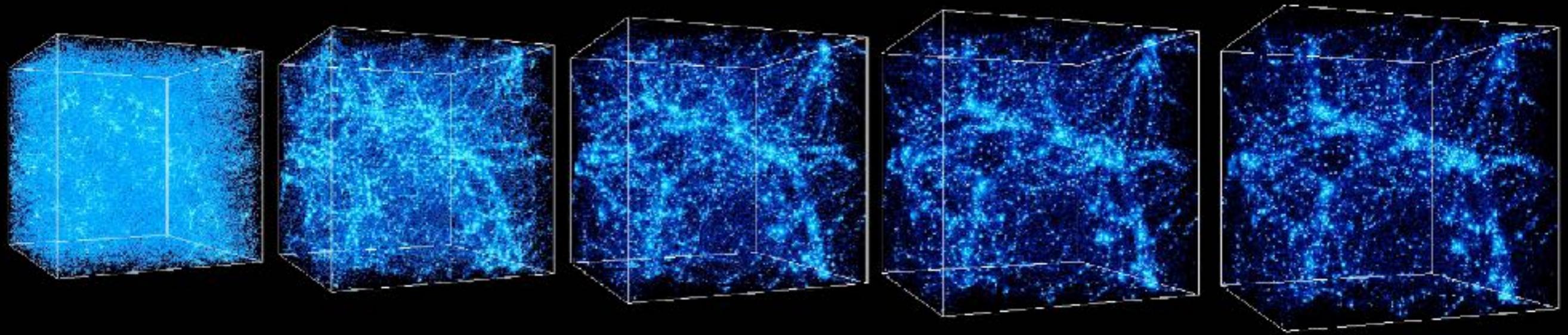
Ω_Λ

Ω_M

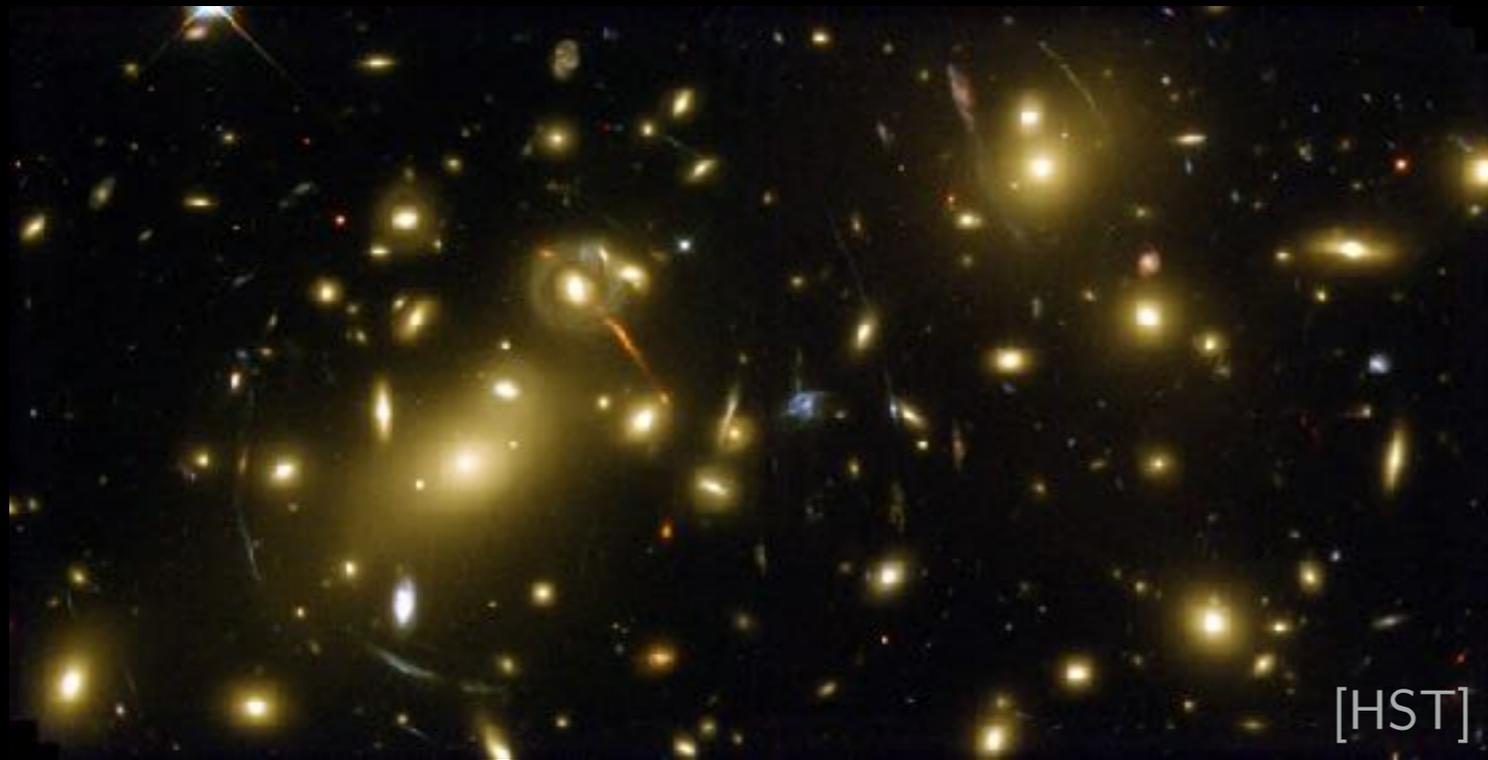
Ω_R

cosmological principle

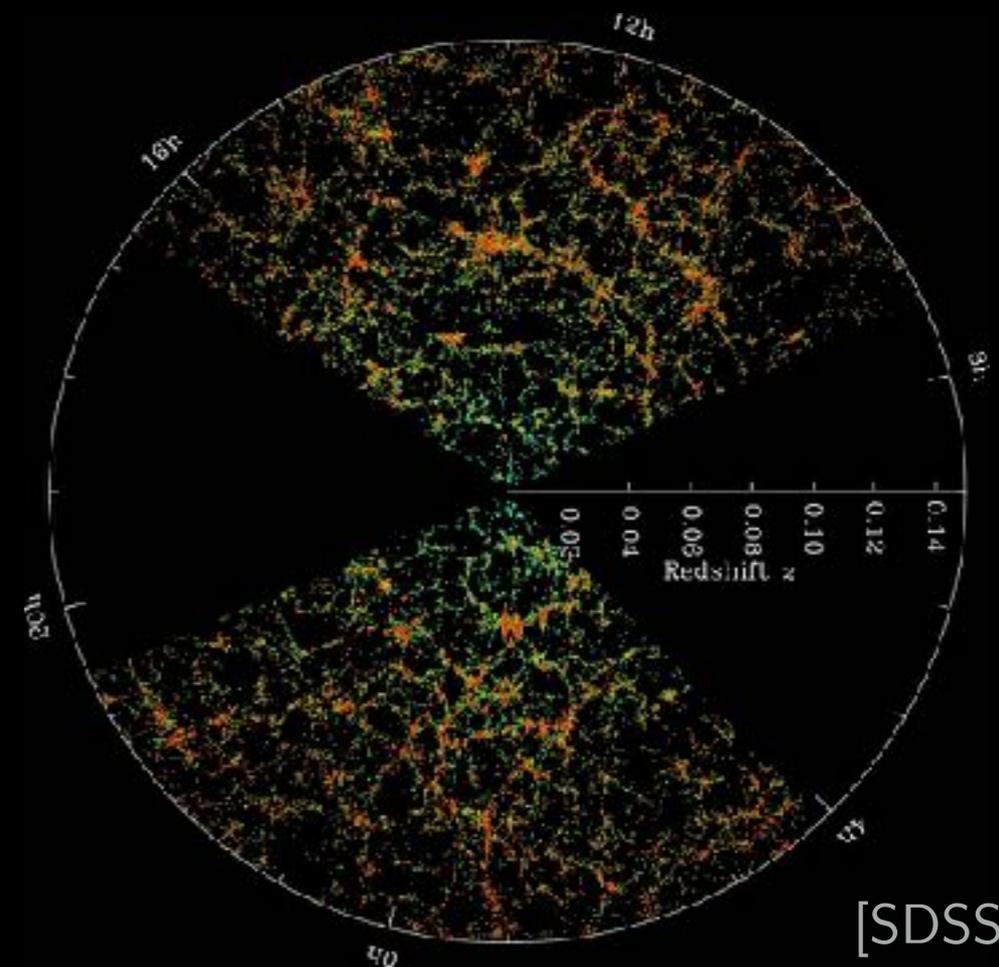
general relativity



[Kravtsov]

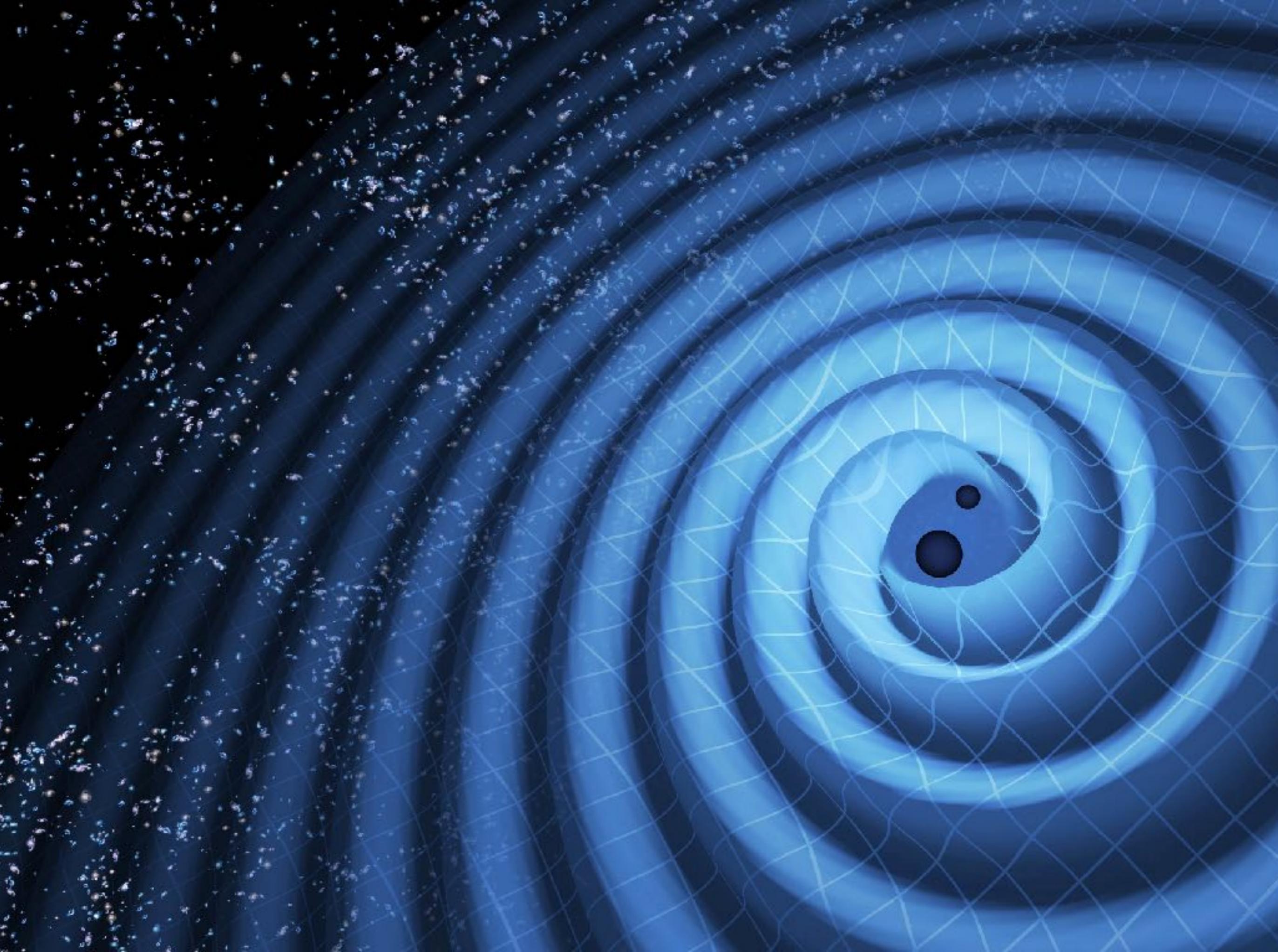


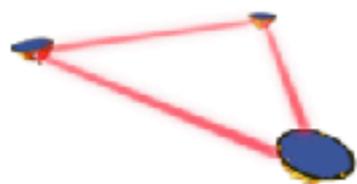
[HST]



[SDSS]

For a review see e.g. [Ferreira '19](#)





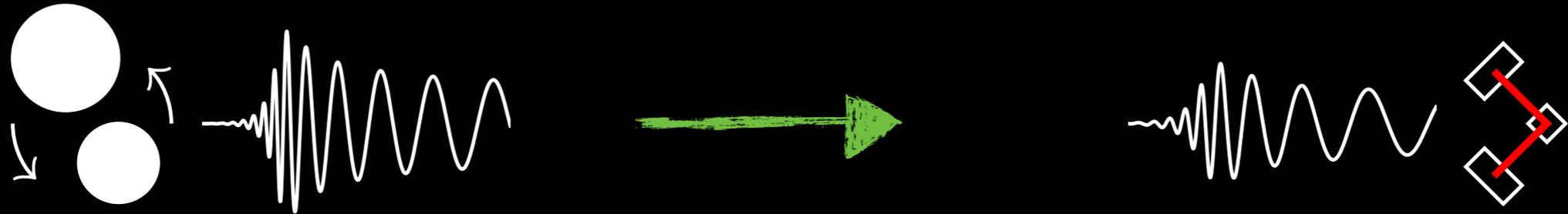
8. Interpretation, key-science projects

WP	Description	Priority
8.1	analysis of joint GW+EM observations of GBs (including VBs)	3
8.2	population studies of GW-only GBs	3
8.3	studies of seed black holes and BH formation mechanisms	3
8.4	studies of SMBHBs and connection to galaxy clustering	3
8.5	analysis of joint EM+GW SMBHB events	3
8.6	analysis of EMRI population	3
8.7	tests of GR and the nature of compact objects	3
8.8	analysis of IMBHBs and IMRIs	3
8.9	studies of SOBH populations	3
8.10	estimation of cosmological parameters	3
8.11	characterisation of backgrounds	3
8.12	analysis of detected unmodelled events	3

Table 8: Work packages on interpretation and key science questions.

Galactic
Cosmology related

Cosmological GW propagation



$$h''_A + 2\mathcal{H}h'_A + c^2k^2h_A = 0$$

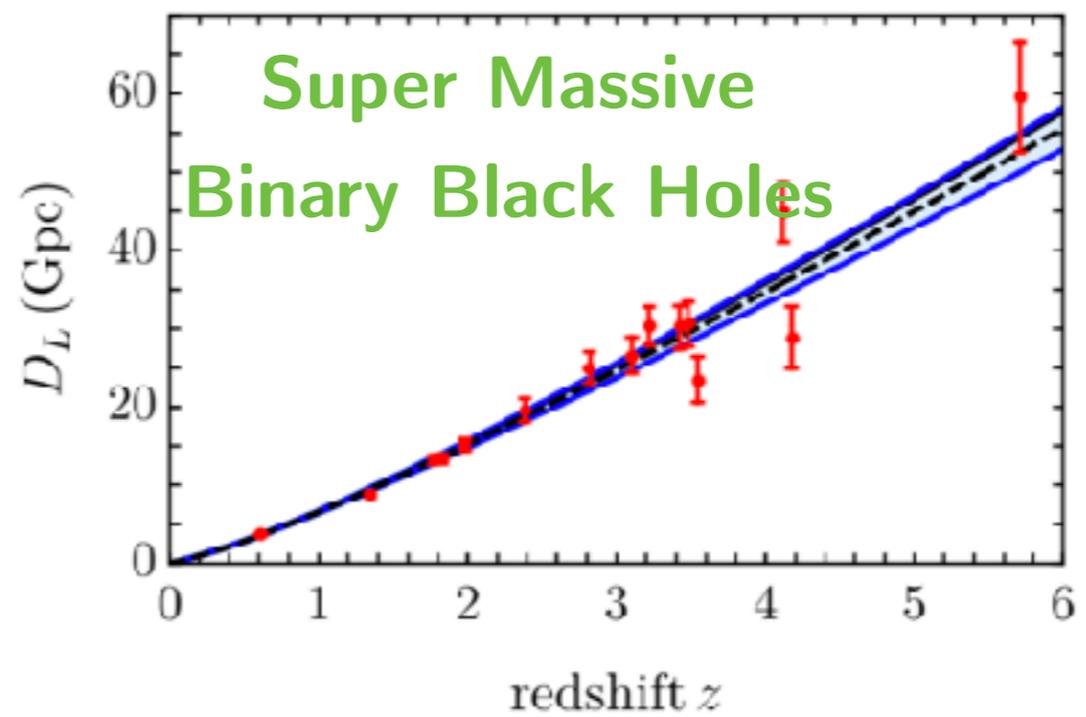
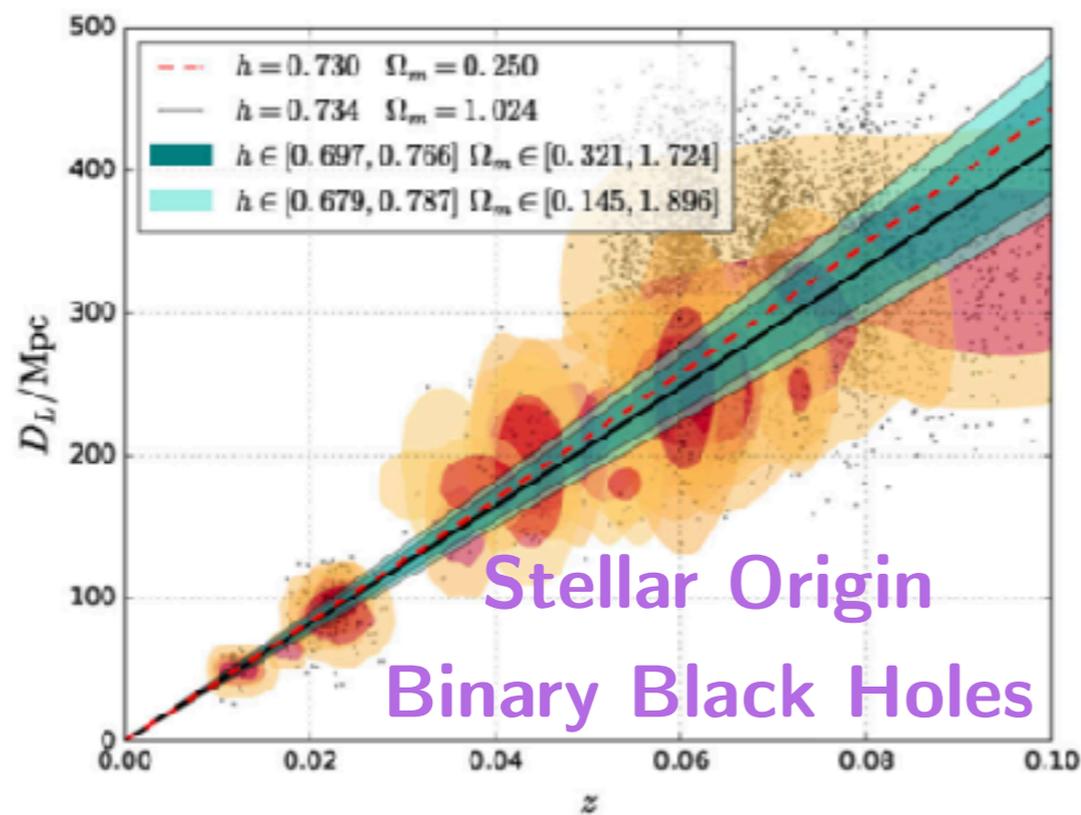
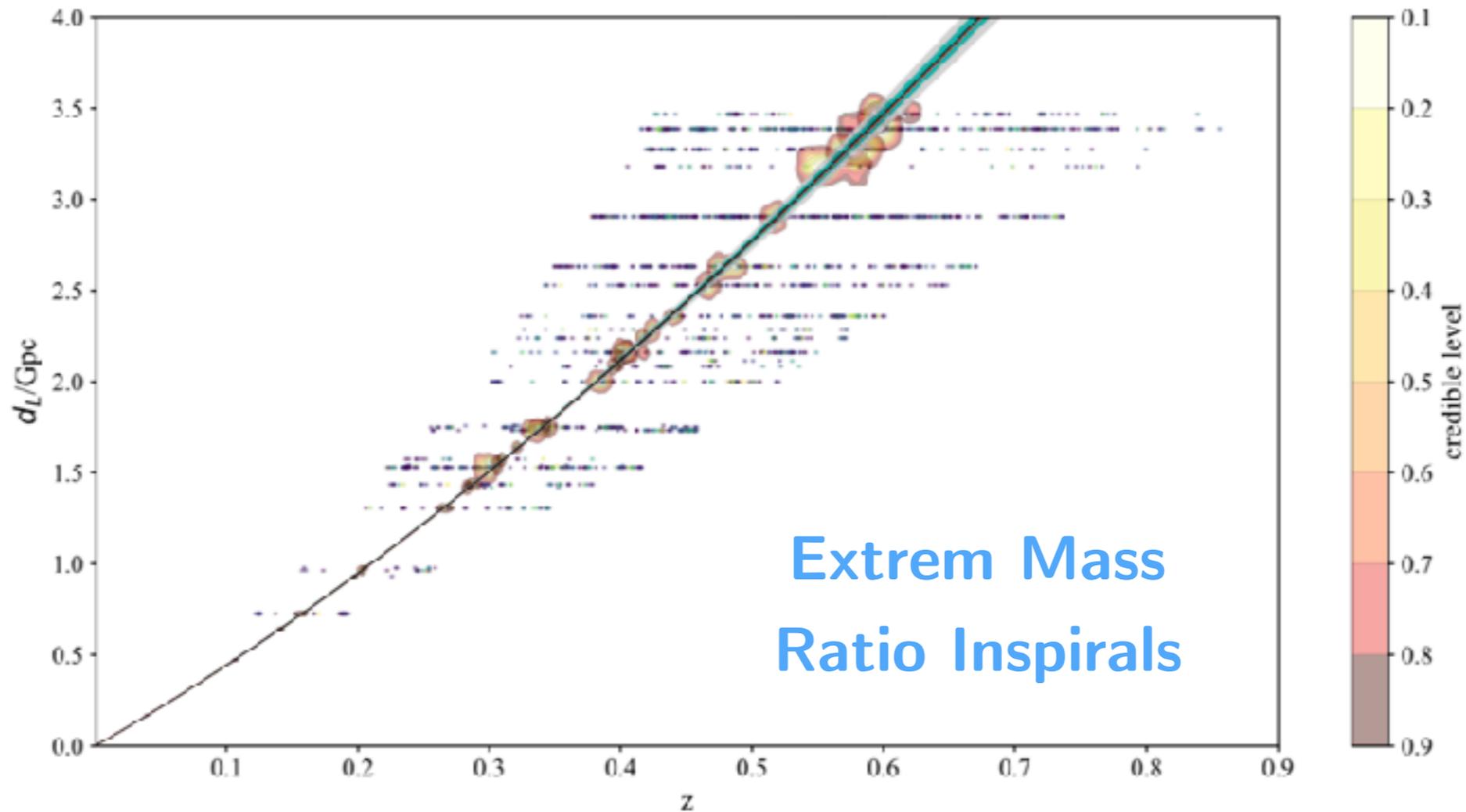
- **Expansion rate:** changes GW amplitude

$$d_L = (1 + z) \int_0^z \frac{cdz}{H(z)}$$

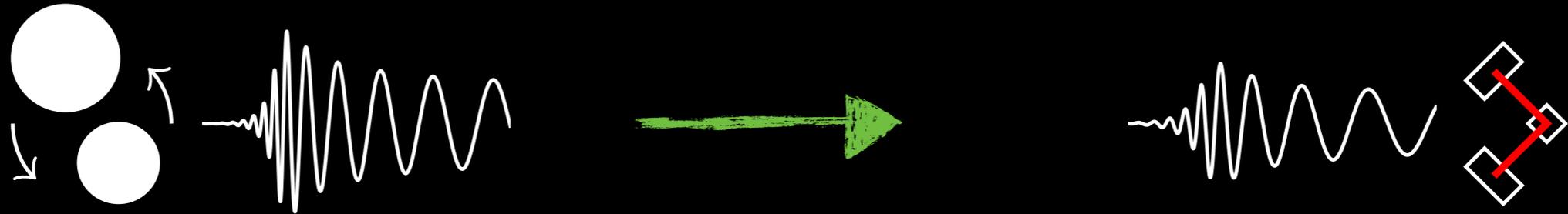
LISA will constrain expansion history at different redshifts, e.g. H_0 , EoS of DE, DM

For more details see:

LISA Cosmology White Paper ([arXiv 2204.05434](https://arxiv.org/abs/2204.05434))



Modified GW propagation



$$h''_A + (2 + \nu) \mathcal{H} h'_A + (c_g^2 k^2 + \Delta\omega) h_A = \mathcal{O}_{AB} h_B$$

- **Speed**: changes arrival time
- **Amplitude**: modifies luminosity distance
- **Phase**: may produce waveform distortions
- **Polarization**: birefringence, additional tensor modes

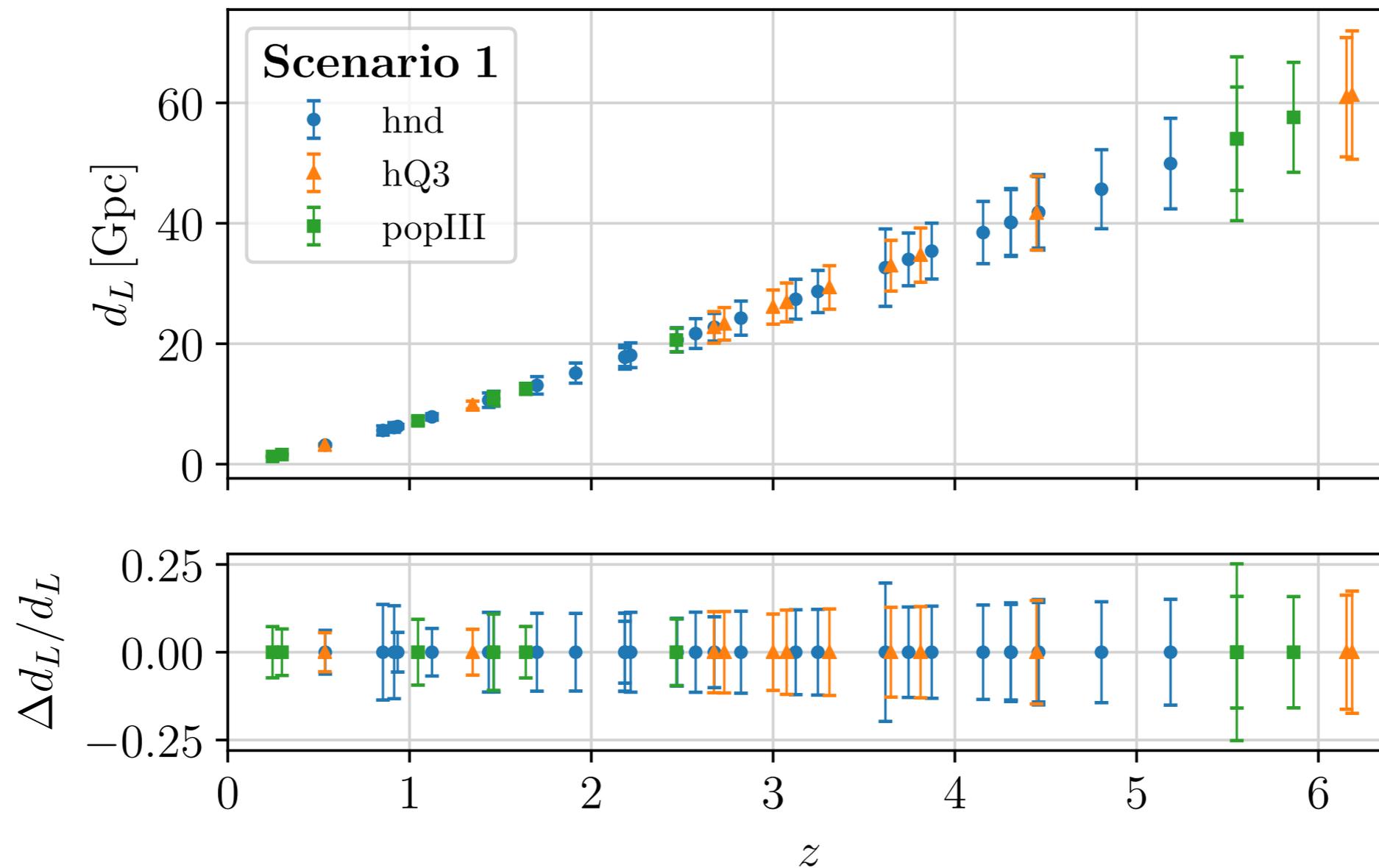
Small deviations accumulate over cosmological propagation times!

For propagation effects beyond cosmological backgrounds:

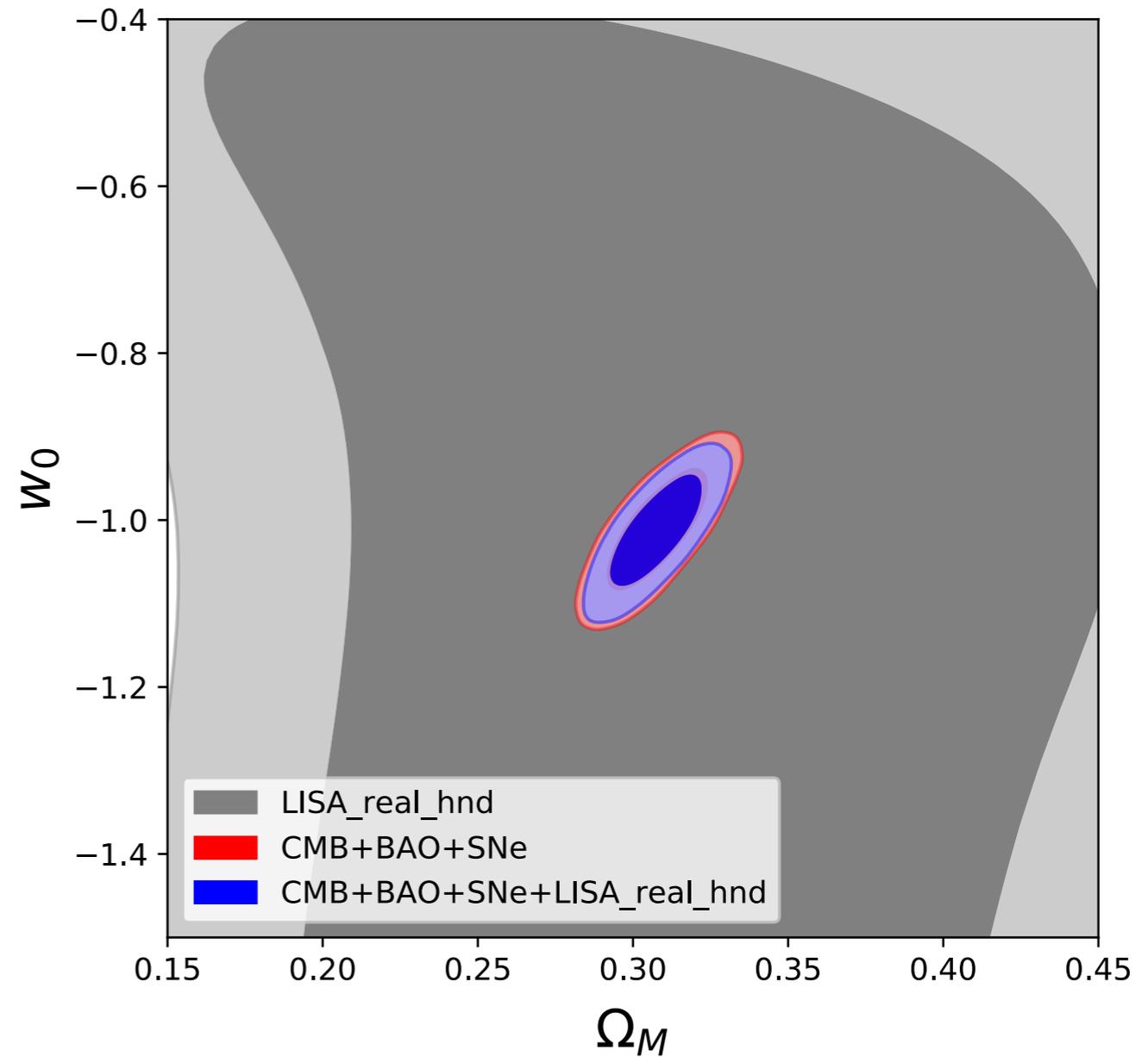
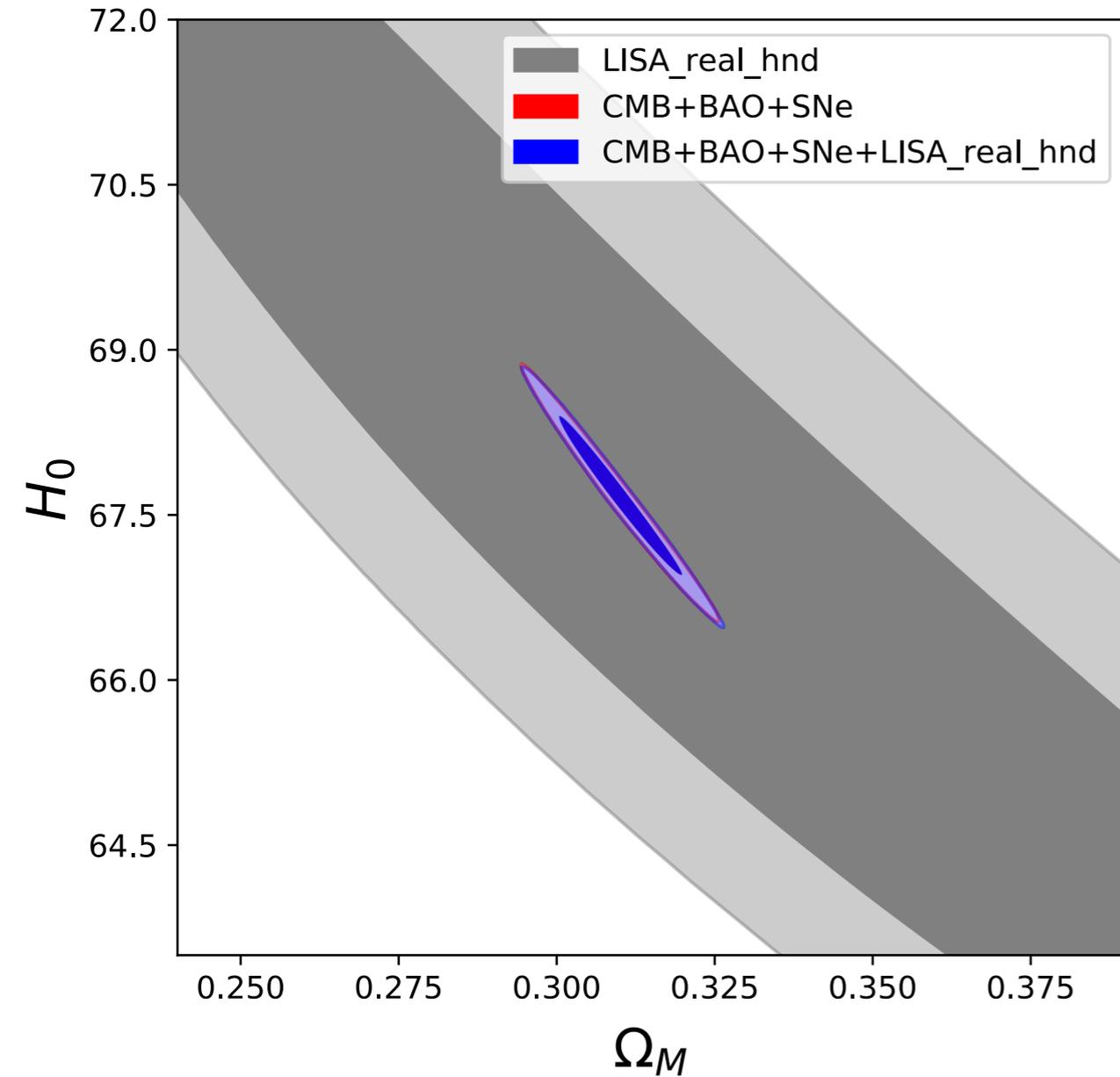
Ezquiaga & Zumalacárregui; *GW lensing beyond GR* (PRD, [arXiv 2009.12187](https://arxiv.org/abs/2009.12187))

LISA forecasts: SMBBHs

[approx. 10-30 bright sirens (4 yrs)]

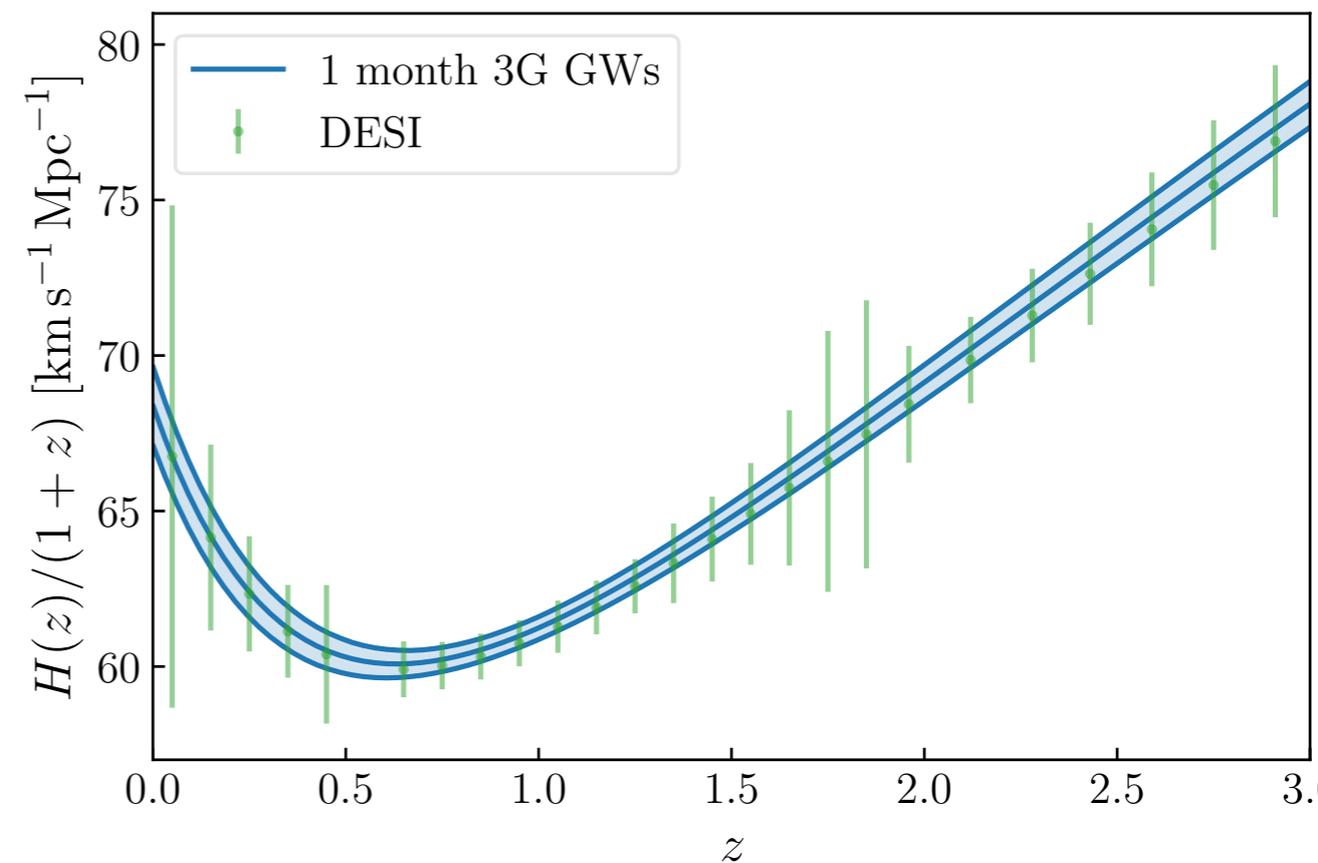
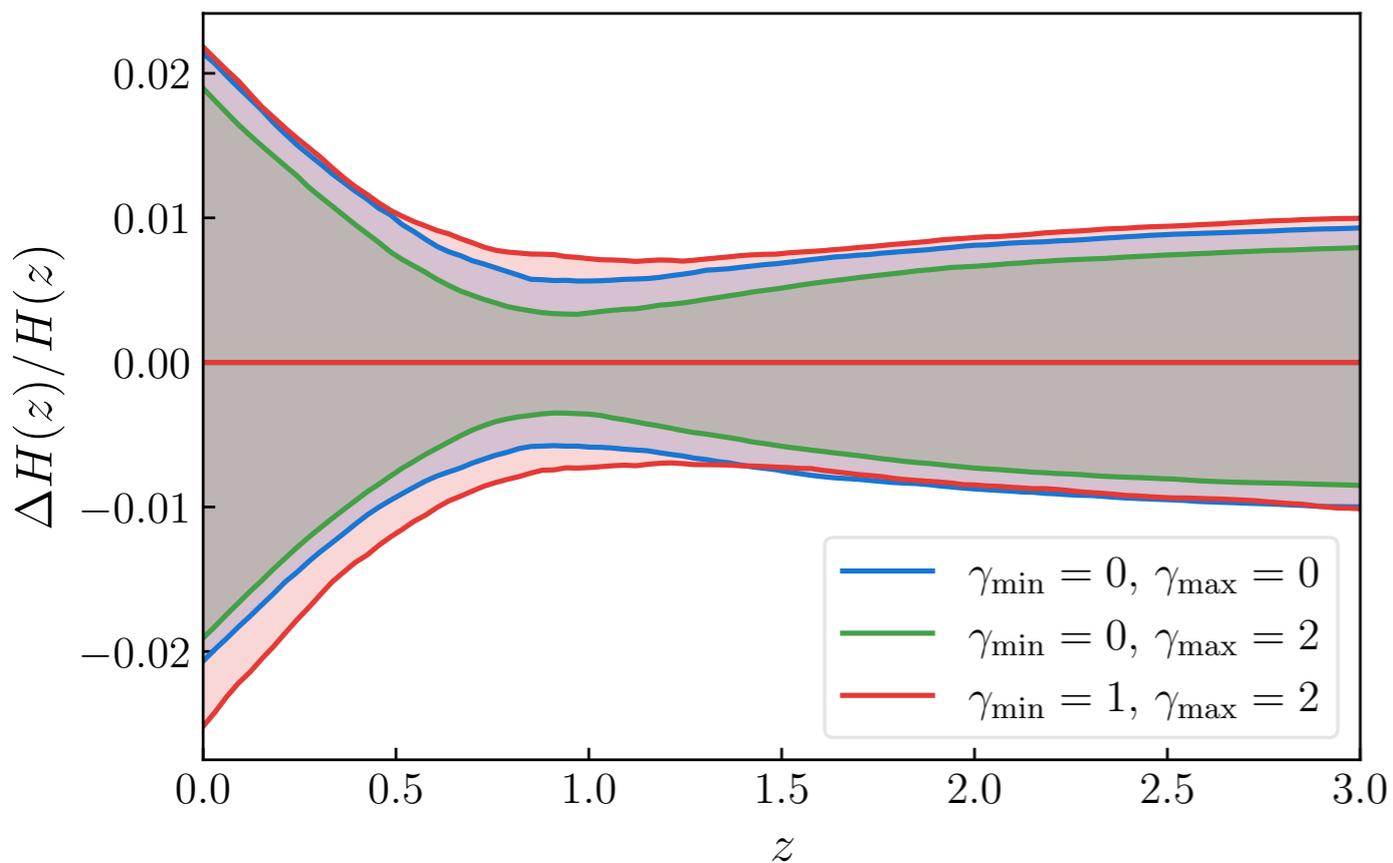


LISA forecasts: SMBBHs



3G cosmo inference

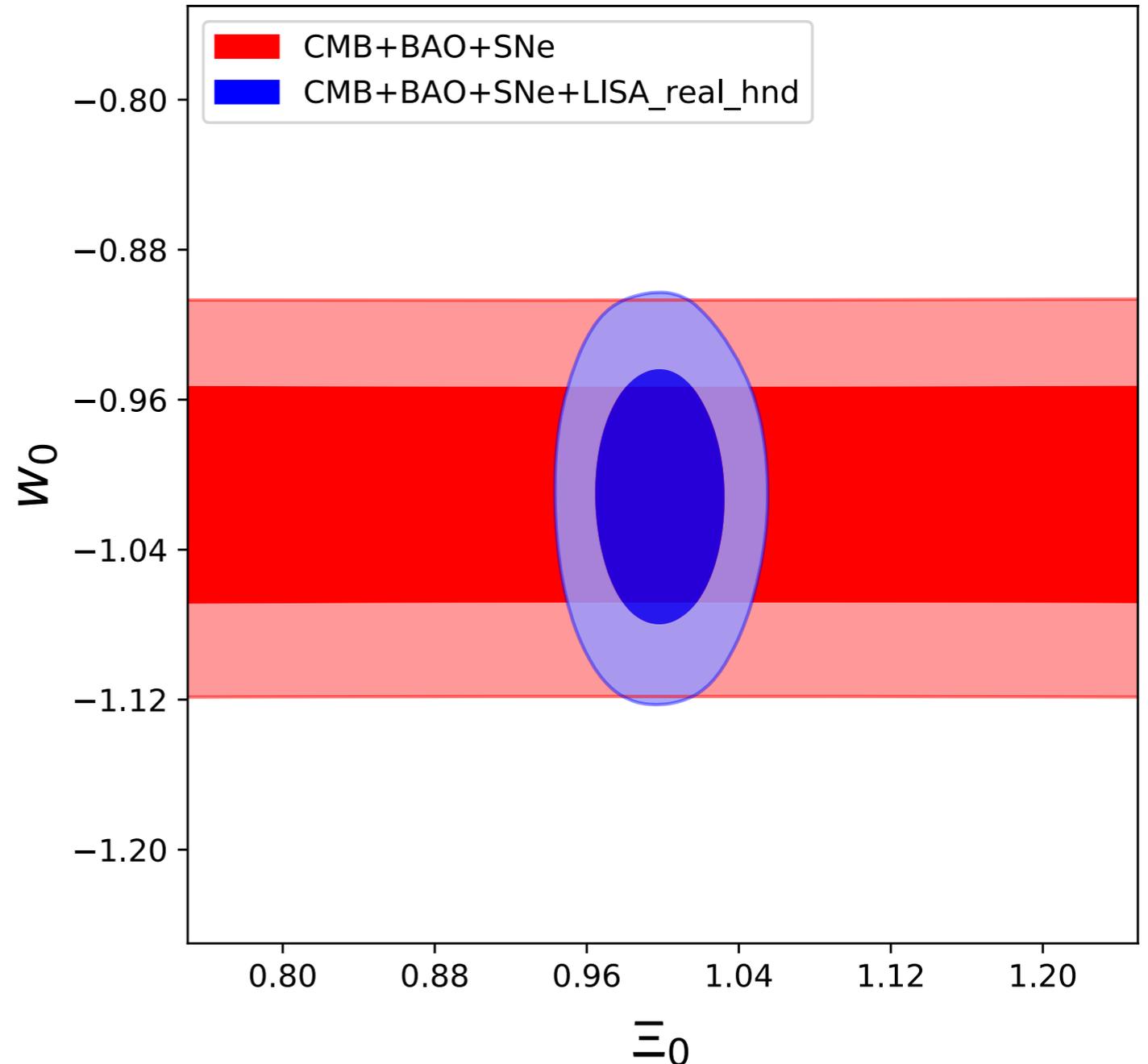
[10,000 **BBHs** between NSBH and PISN gap (1 month)]



Sub-percent within 1 month. High-redshift!

LISA forecasts: SMBBHs

$$\frac{d_L^{\text{gw}}}{d_L^{\text{em}}} = \Xi_0 + \frac{1 - \Xi_0}{(1+z)^n}$$



Modified dispersion relation (MDR)

General relativity predicts:

$$\omega(k) = c \cdot k$$

Massive graviton:

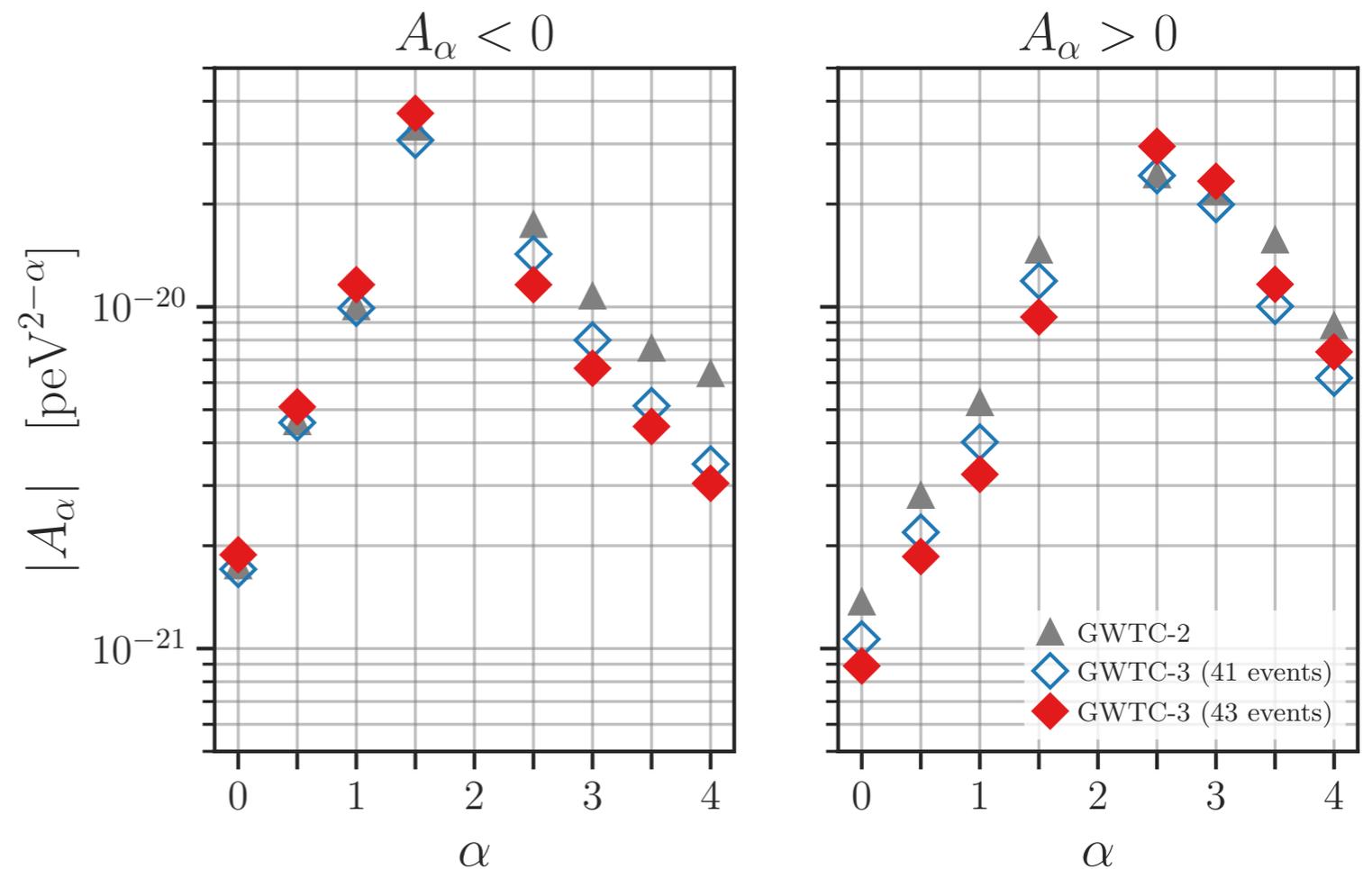
$$\omega^2 = c^2 k^2 + m^2 c^4$$

[Will'98]

General MDR:

$$\omega^2 = c^2 k^2 + \Lambda (ck)^\alpha$$

[Mirshekari et al.'11]

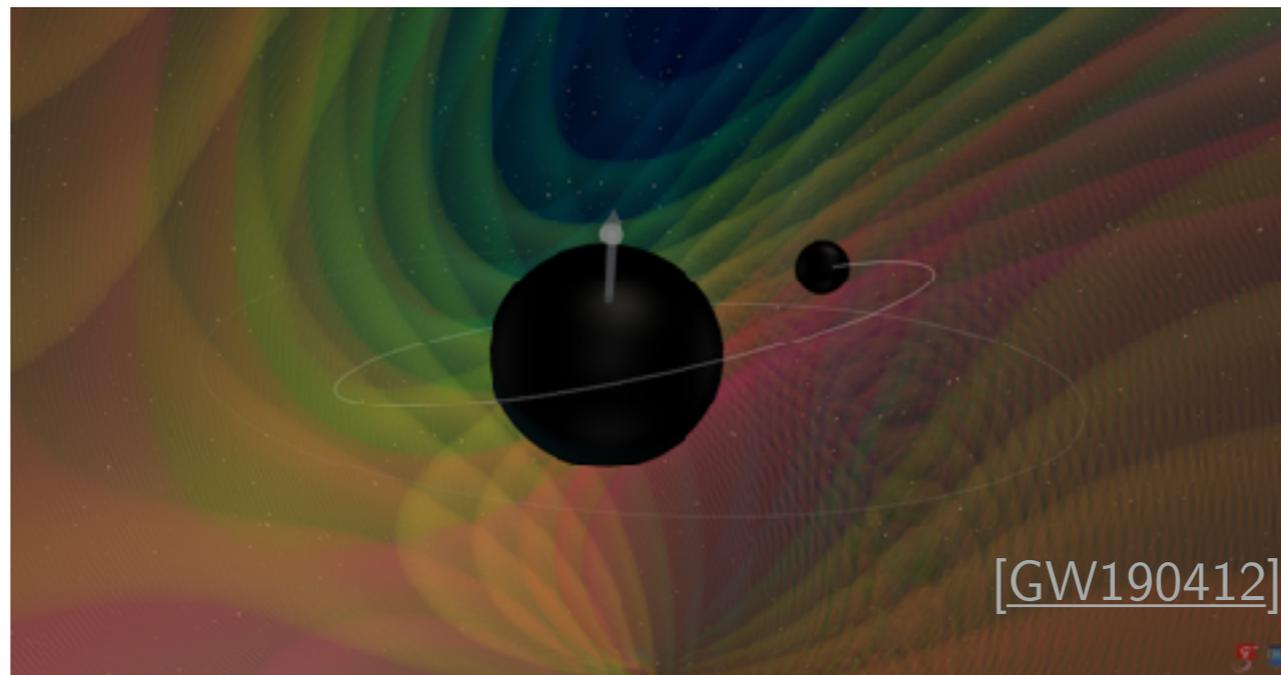


MDR with higher modes

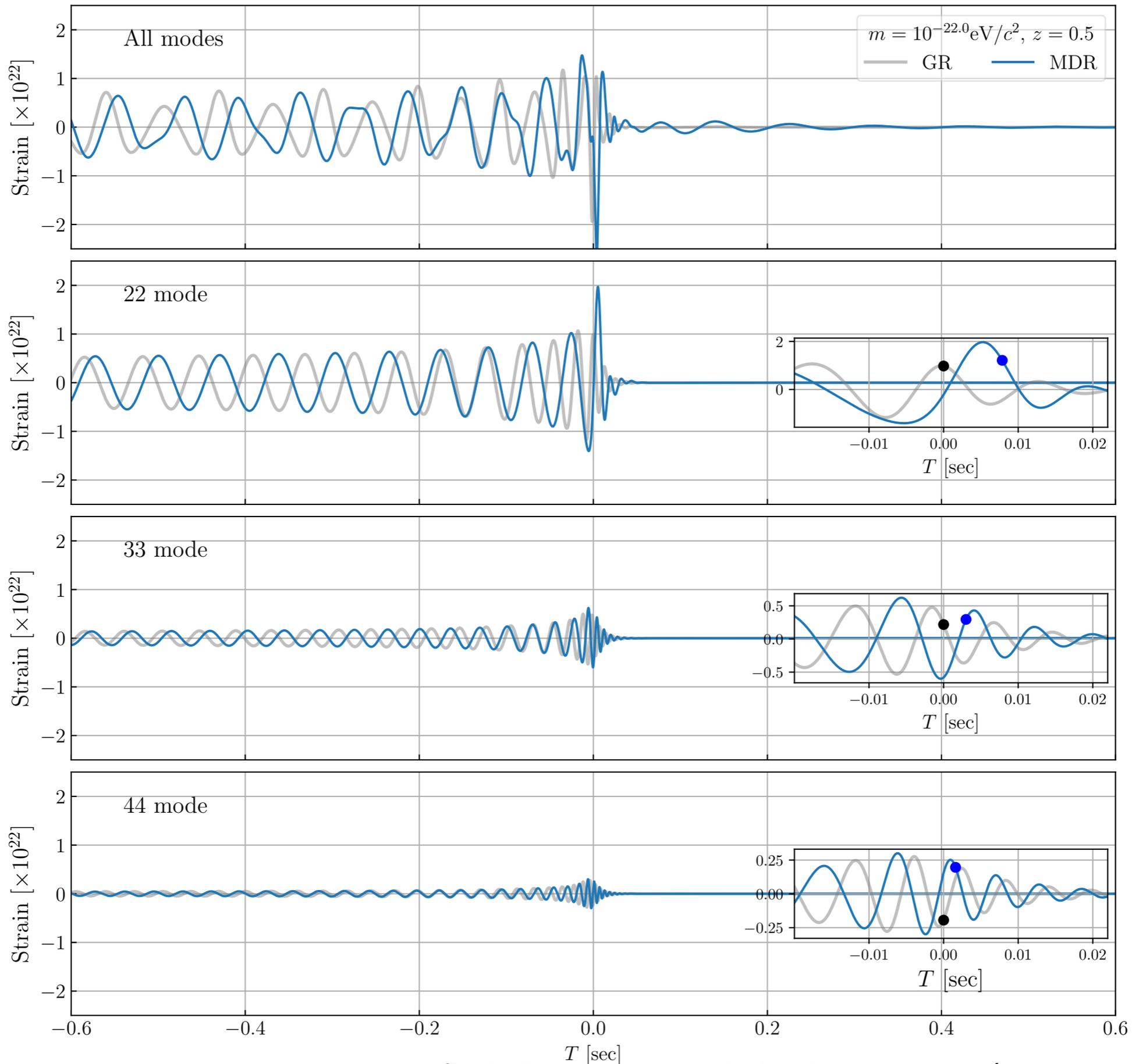
Previously, only dominant quadrupole ($l,m=2,2$) mode included.

Frequency-independent phase shifts are *degenerate* with coalescence phase

We have now events with evidence of HMs, *definitely* more with LISA



Each higher modes gets a different time delay and phase shift!



MDR with higher modes

Solving the propagation equations using **WKB** allows for arbitrary initial conditions

[Ezquiaga et al.'21]

$$h_{\text{mg}} \sim h_{\text{gr}} e^{-i \int \Delta\omega dz / H(z)} \equiv h_{\text{gr}} e^{i\Delta\Psi} \quad \Delta\Psi(f) = -\frac{\Lambda}{2} D_\alpha (2\pi f_s)^{1-\alpha}$$

WKB approach is equivalent to the stationary phase approximation (SPA) with time delays computed with the **group velocity**

This is different to the SPA with **particle velocity**

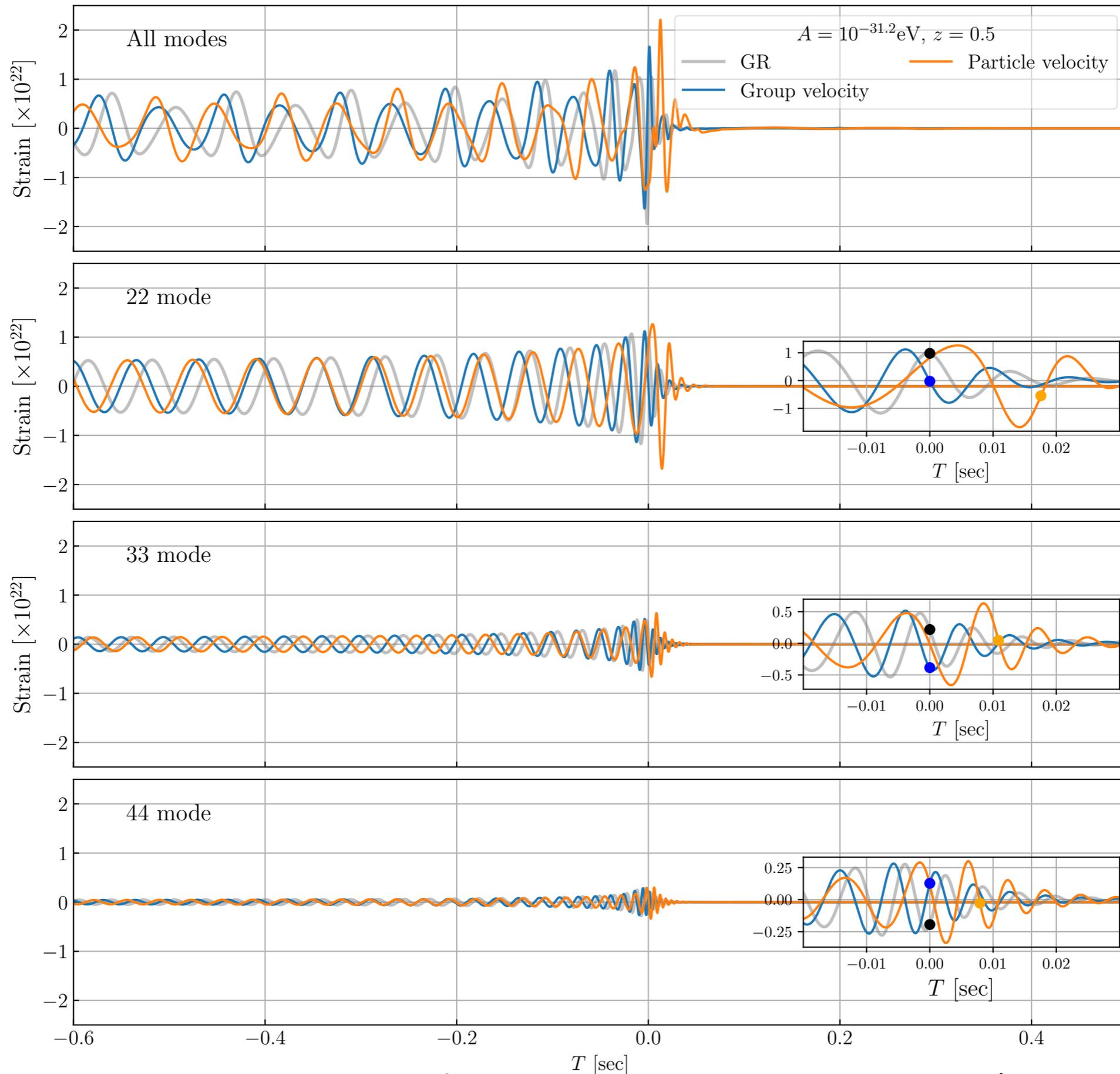
E.g. $\omega^2 = c^2 k^2 + \Lambda ck$:

$$\Delta\Psi(f) = -\frac{1}{2}\Lambda D_1$$

group velocity

$$\Delta\tilde{\Psi}(f) = \frac{1}{2}\Lambda D_1 \ln\left(\frac{ef}{f_0}\right)$$

particle velocity

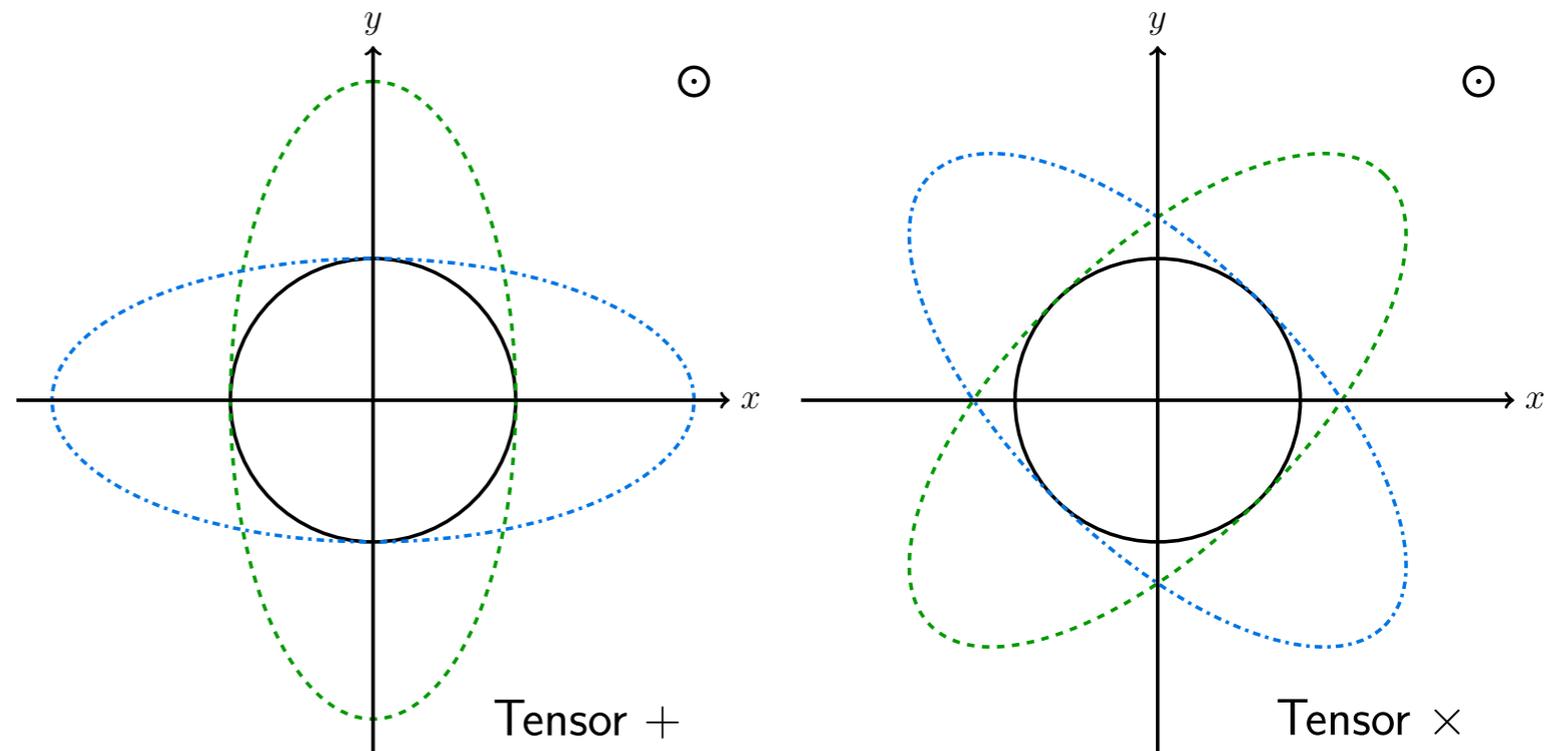


Polarization

Gravitational Wave Polarizations

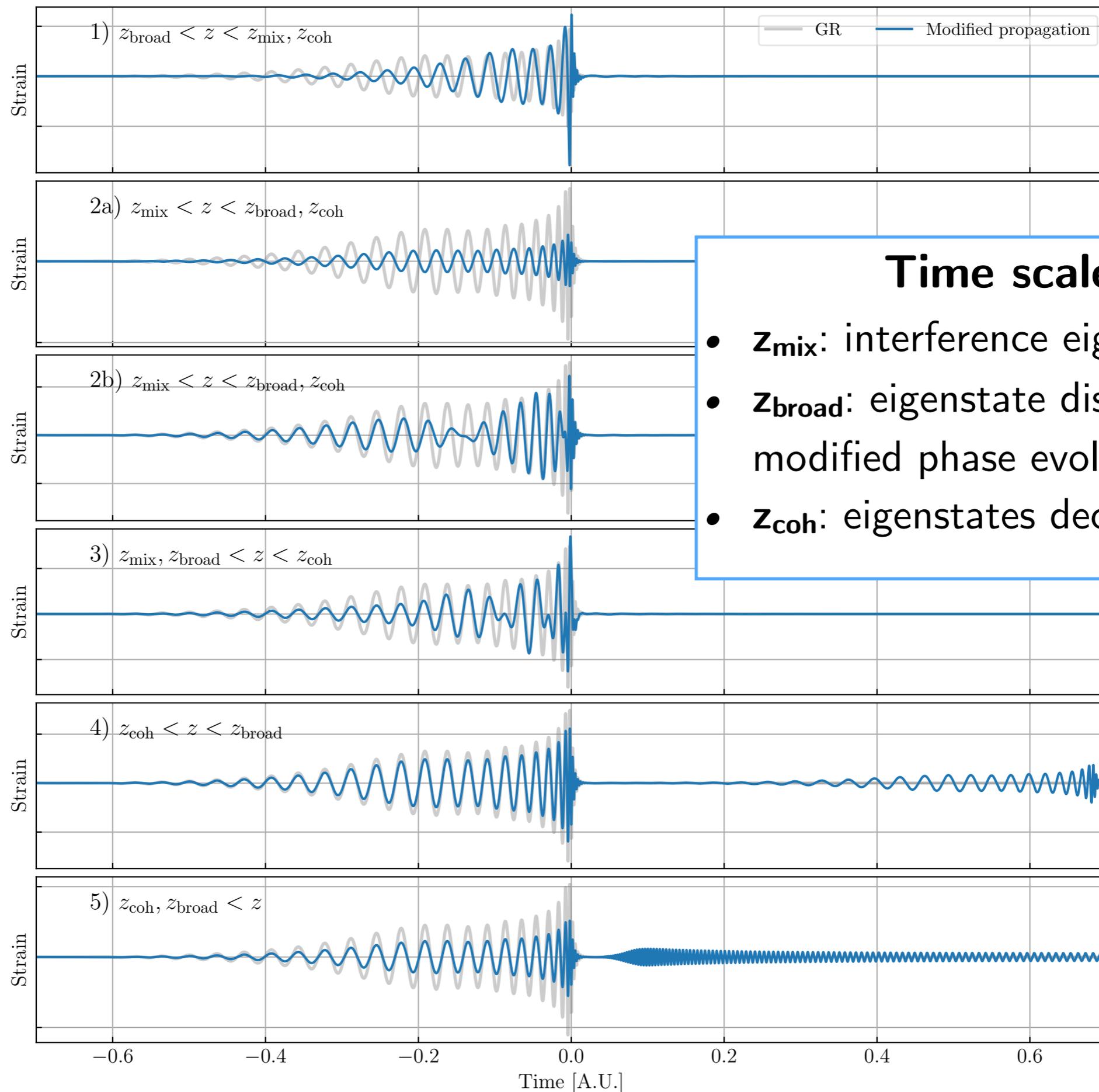
General relativity predicts:

$$h_+, \quad h_\times$$



Mixing cosmological tensor fields (similar to neutrino oscillations)

$$\left[\hat{I} \left(\frac{d^2}{d\eta^2} + (ck)^2 \right) + \begin{pmatrix} m_h^2 & m_{hs}^2 \\ m_{hs}^2 & m_s^2 \end{pmatrix} \right] \begin{pmatrix} h_{+, \times} \\ s_{+, \times} \end{pmatrix} = 0$$



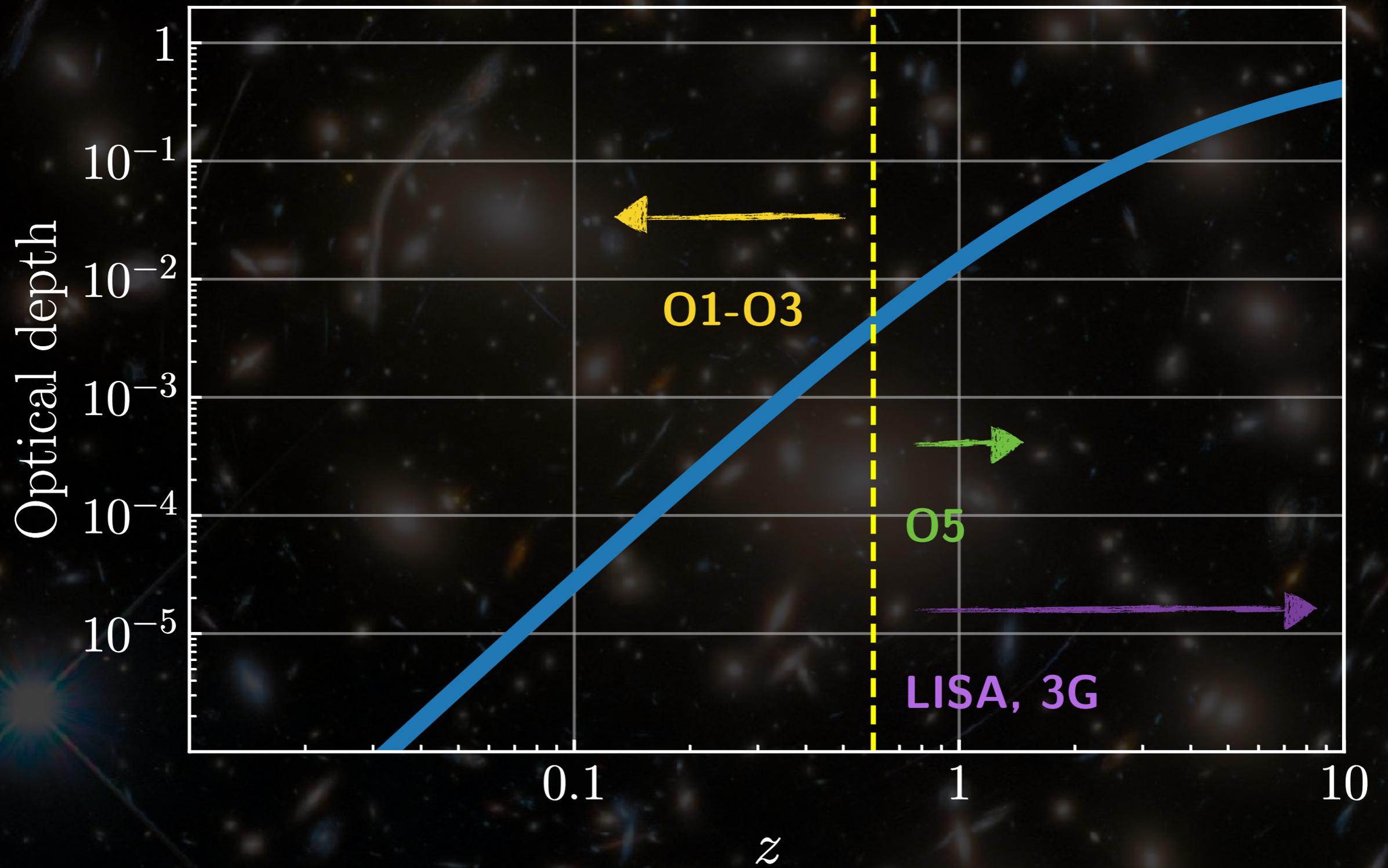
Open questions

What are we learning about dark energy with these parameterizations?

Can we treat each effect separately?

E.g. luminosity distance vs modified dispersion relation

Propagation effects will likely dominate, but can waveform distortions at emission bias these analyses? Screening!

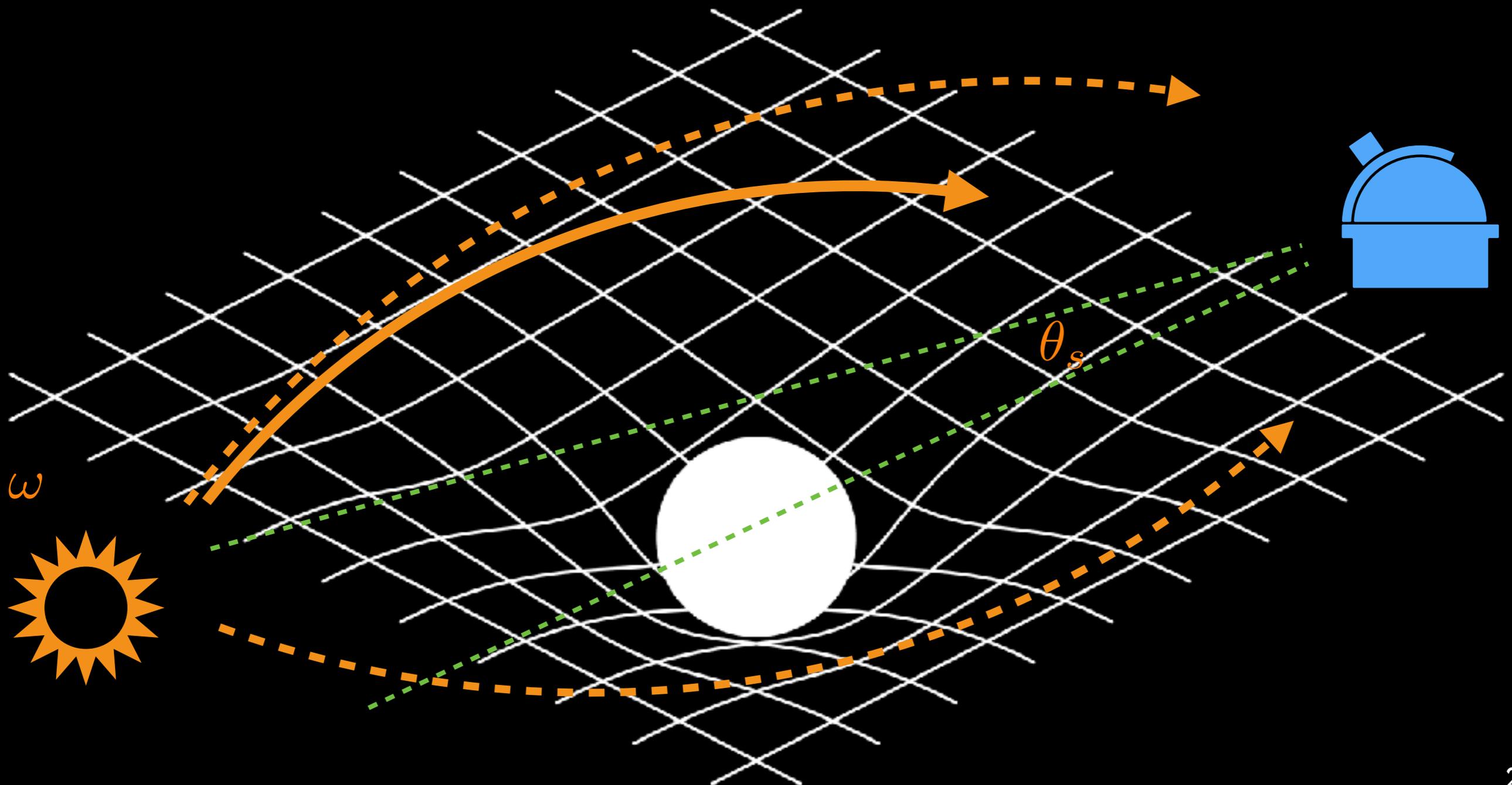


Solving lensing

$$\Delta t_d \cdot \omega$$

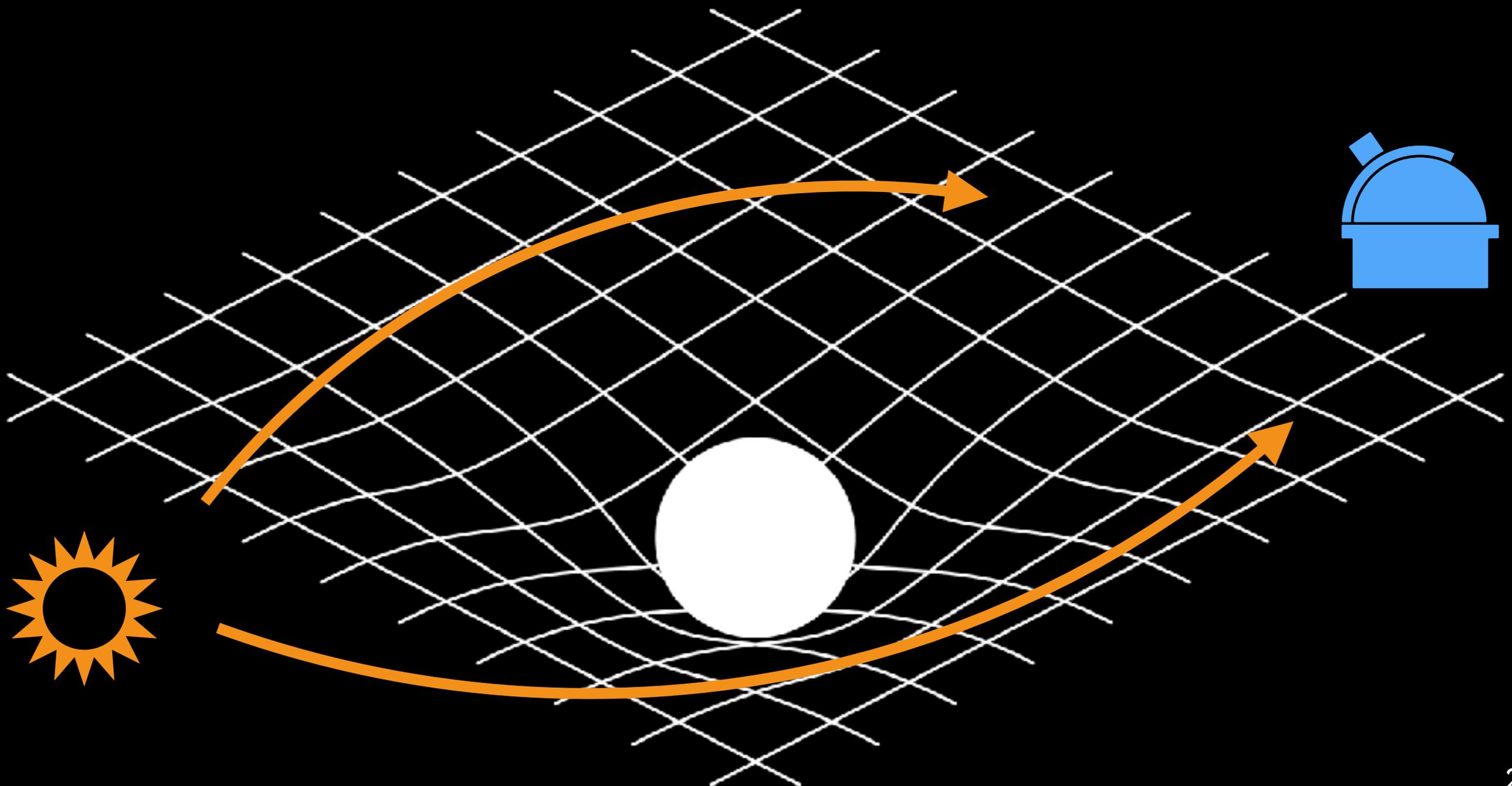
$$h_L(\omega, \theta_s) = F(\omega, \theta_s)h(\omega)$$

$$F(\omega, \theta_s) \sim \int d^2\theta e^{i\omega t_d(\theta, \theta_s)}$$



Strong lensing

$$\Delta t_d \cdot \omega \gg 1$$



RXJ1131-1231



B1608+656



HE0435-1223



WFI2033-4723



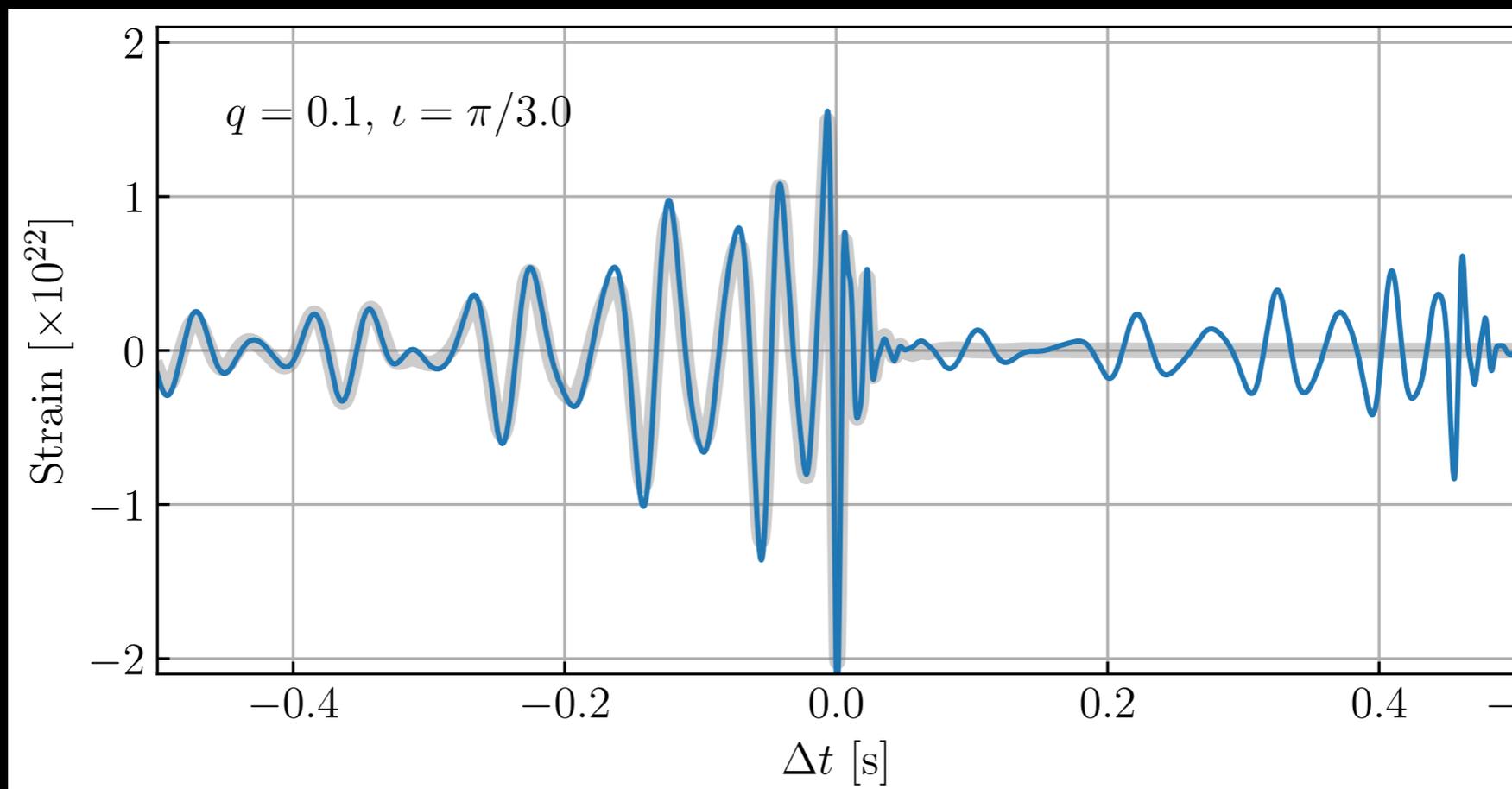
[HST]

Strong lensing

$$\Delta t_d \cdot \omega \gg 1$$

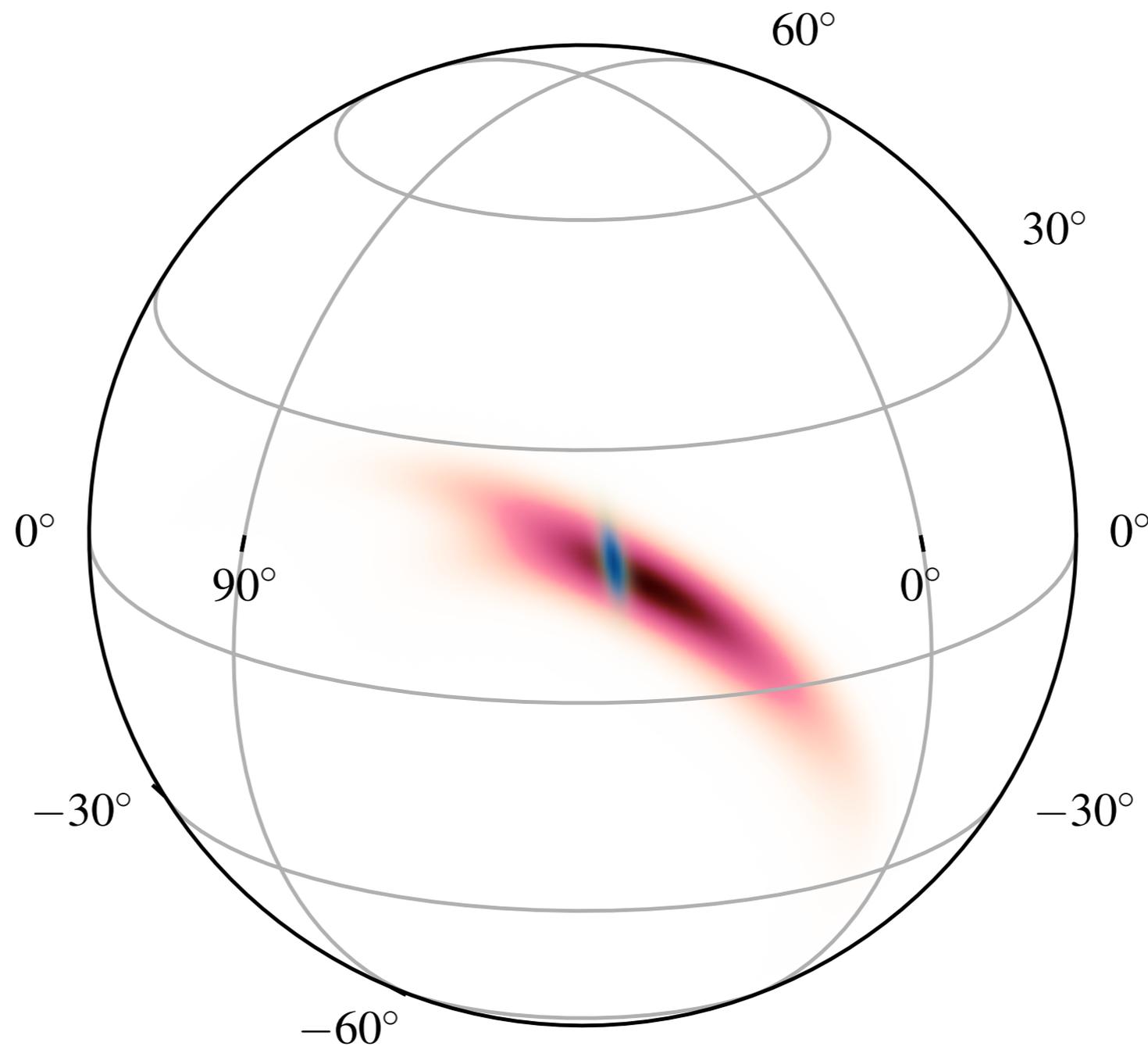
$$F \approx \sum_j |\mu_j|^{1/2} \exp(i\omega t_j - i\pi n_j)$$

Magnification
Time delay
Phase shift



GW sky localization

$$\theta_E \sim 1'' \sqrt{\frac{M}{10^{12} M_\odot}} \sqrt{\frac{1 \text{ Gpc}}{D}}$$



Strong lensing

$$\Delta t_d \cdot \omega \gg 1$$

$$F \approx \sum_j |\mu_j|^{1/2} \exp(i\omega t_j - i\pi n_j)$$

Magnification
Time delay
Phase shift

- Each image type acquire a different phase shift

$$n_j = 0, 1/2, 1$$

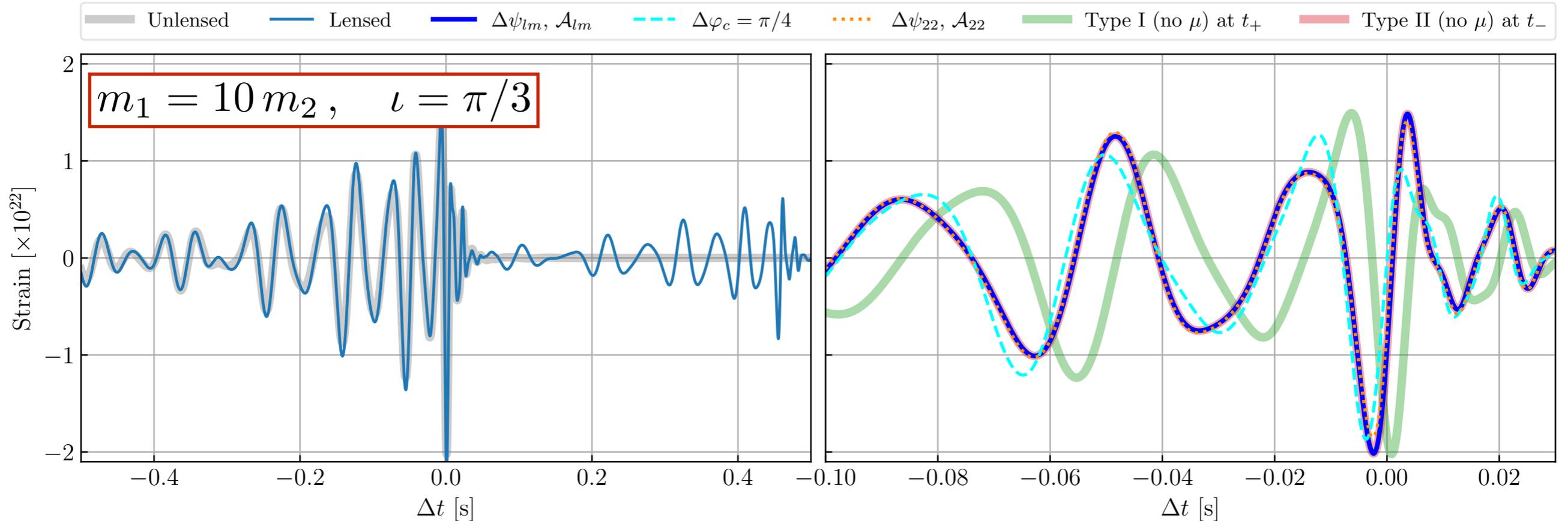
- A frequency independent phase shift is equivalent to a frequency dependent time delay

$$\Delta t_j = \pi n_j / \omega$$

Waveform distortions

$$h = \sum_{l,m} \mathcal{A}_{lm} \cos [m(\Omega t + \varphi_c) - 2\chi_{lm}]$$

$$\Delta t = n_j \pi / |\omega|$$



Strong lensing

$$\Delta t_d \cdot \omega \gg 1$$

$$F \approx \sum_j |\mu_j|^{1/2} \exp(i\omega t_j - i\pi n_j)$$

Magnification
Time delay
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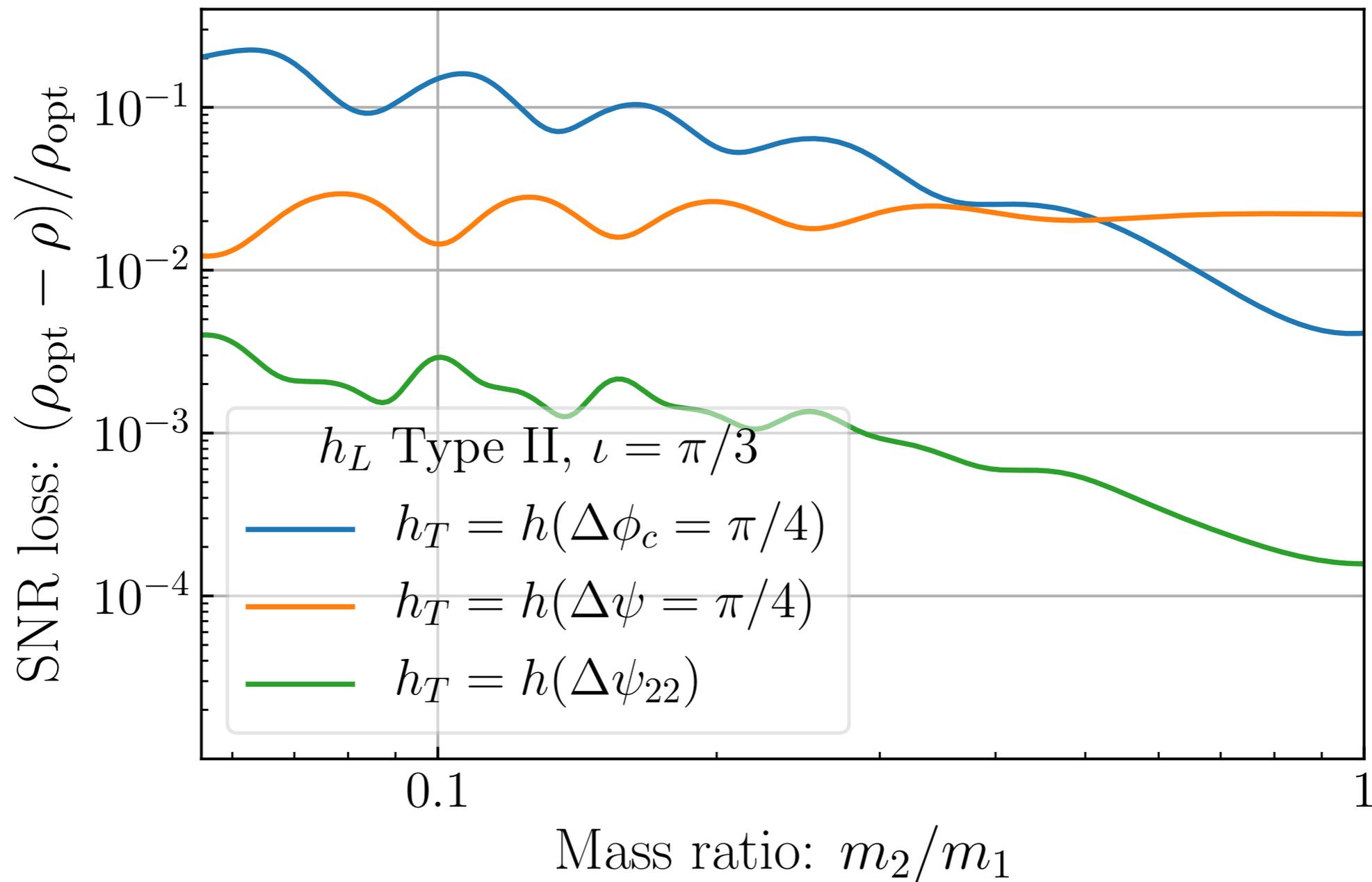
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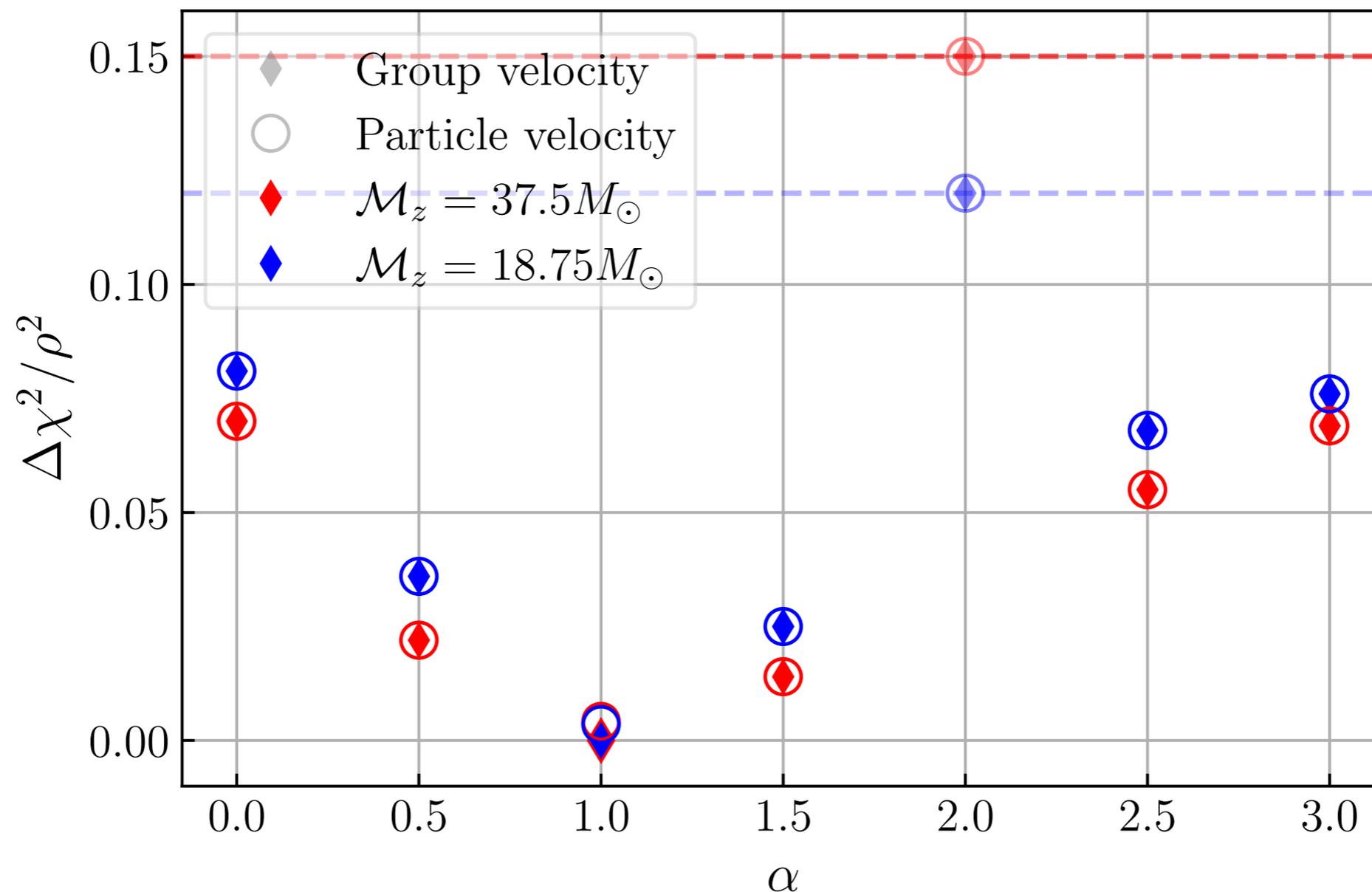
- Lensed GWs *can differ* from (unlensed) GR wave-forms
- *Identify* strong lensing with *single image*

Effect on the SNR



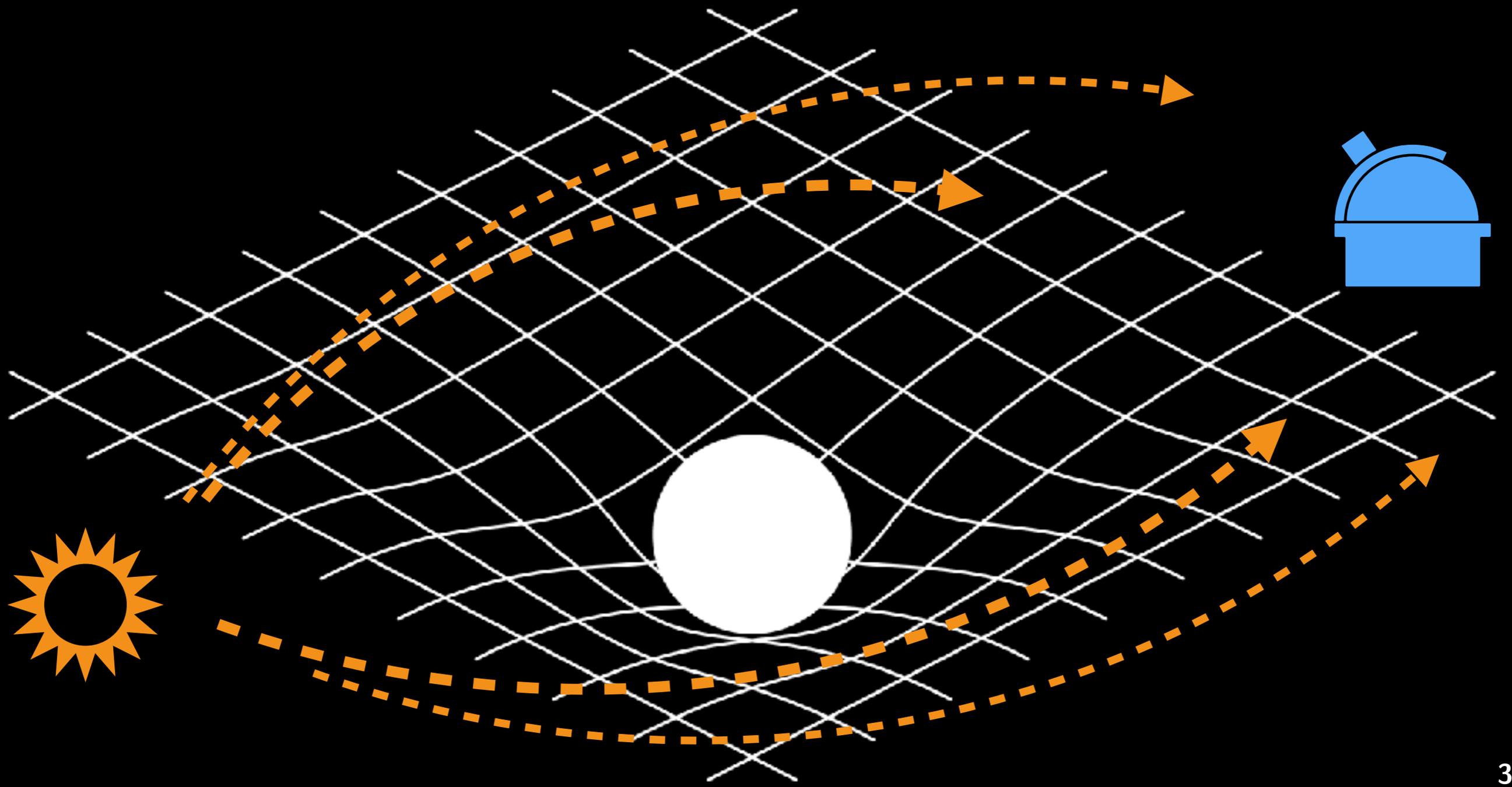
Degeneracies with lensing

- Strong lensing: $F \approx \sum_j |\mu(\vec{\theta}_j)|^{1/2} \exp\left(i\omega t(\vec{\theta}_j) - i\pi \text{sign}(\omega)n_j\right)$

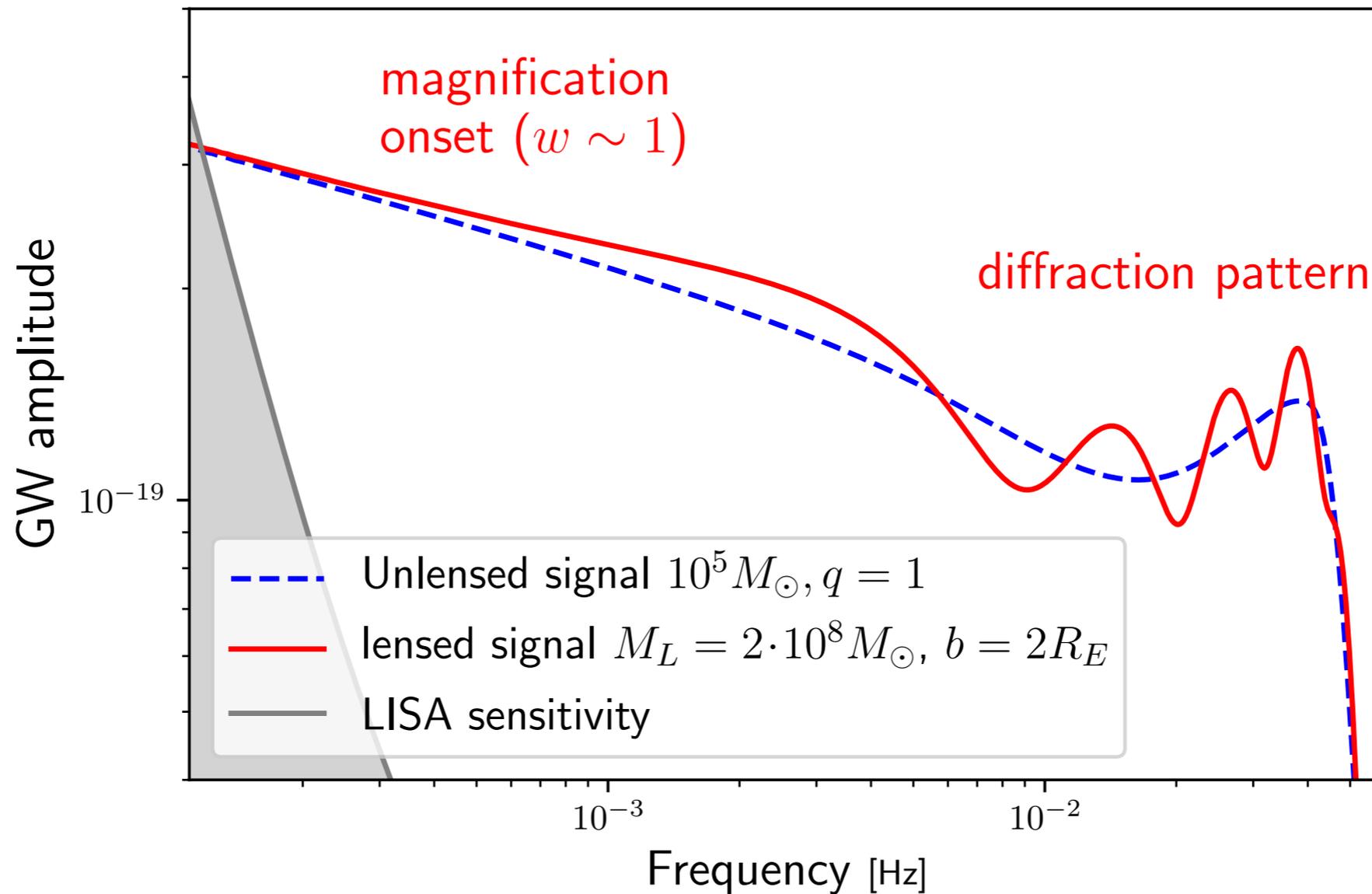


Wave effects

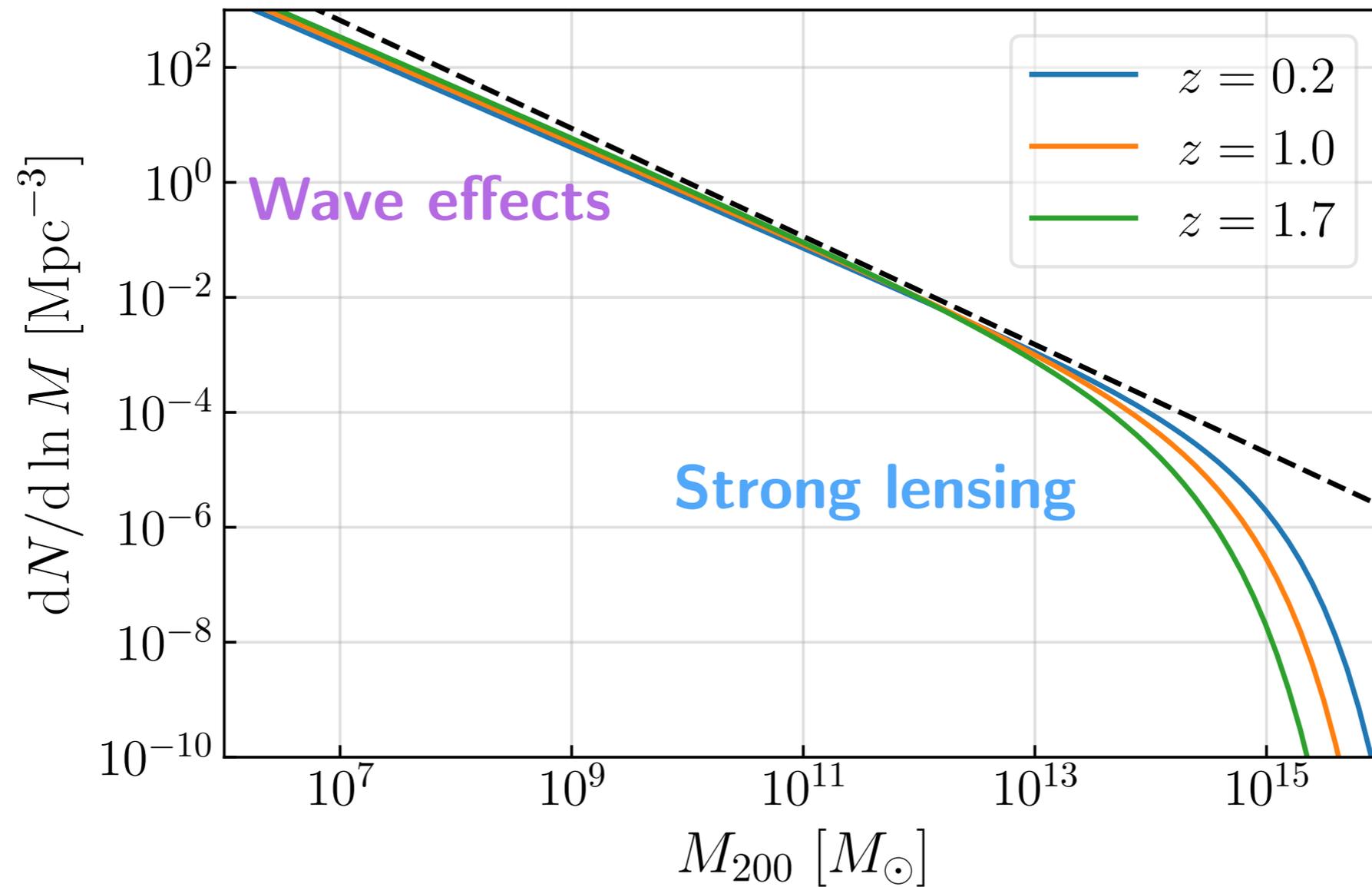
$$\Delta t_d \cdot \omega \lesssim 1$$



Wave effects



Probing matter distribution



Open questions

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Can we treat each effect separately?

E.g. luminosity distance vs modified dispersion relation

Propagation effects will likely dominate, but can waveform distortions at emission bias these analyses? Screening!

Type II image identification with LISA

What types of dark matter halos can be probed?

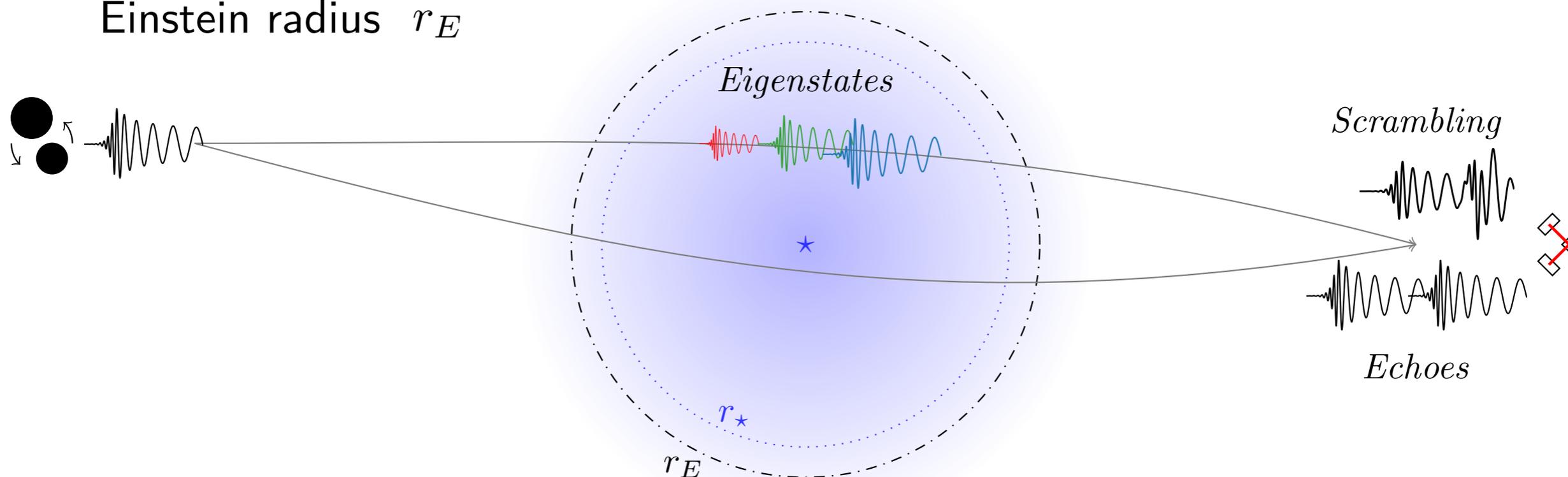
Sereno *et al.* ([arXiv 1011.5238](#)) strong lensing forecasts < 5 events, wave optics negligible

Gao *et al.* ([arXiv 2102.10295](#)) wave optics forecasts: 0.1-1.6% of events

GW lensing beyond GR



- Beyond GR the background of the additional fields $\phi(r)$ modify propagation (besides the change in gravitational potential)
- The relevant scale for the modifications r_* might be different from the Einstein radius r_E



GWs can **mix** with the additional fields. The propagation **eigenstates** may have different speeds, **splitting** or **distorting** each image

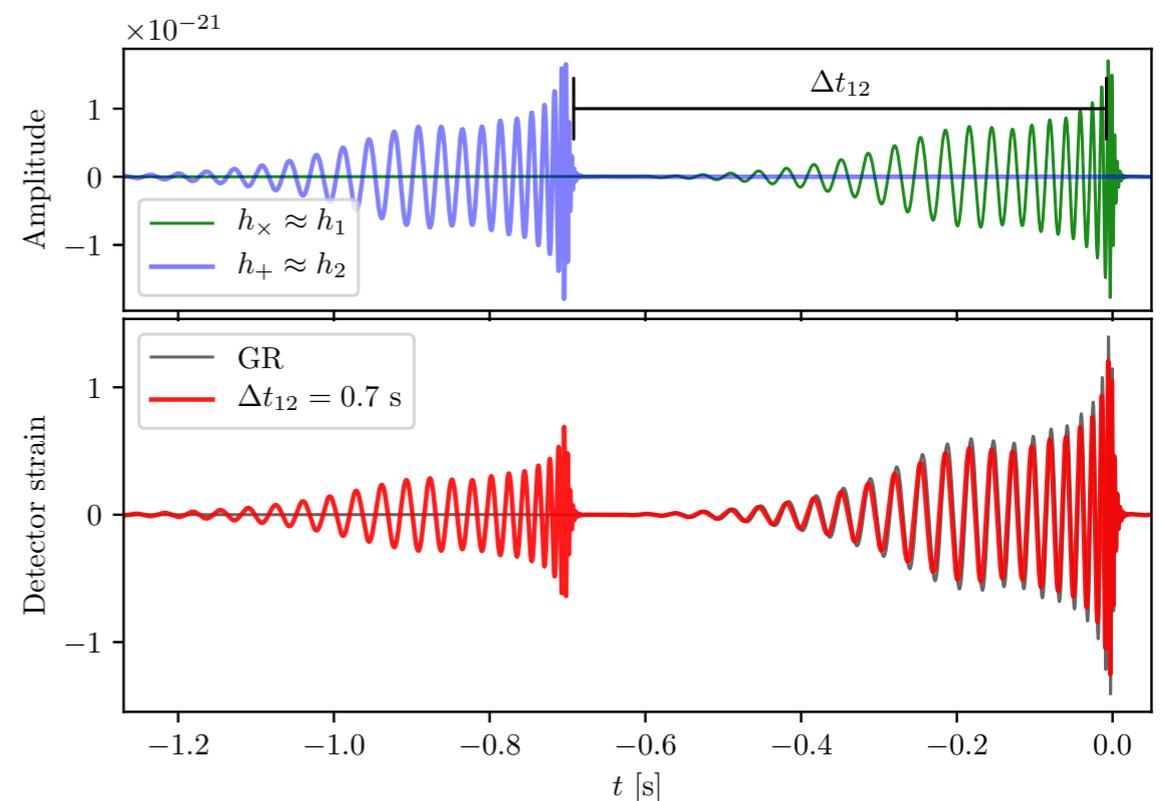
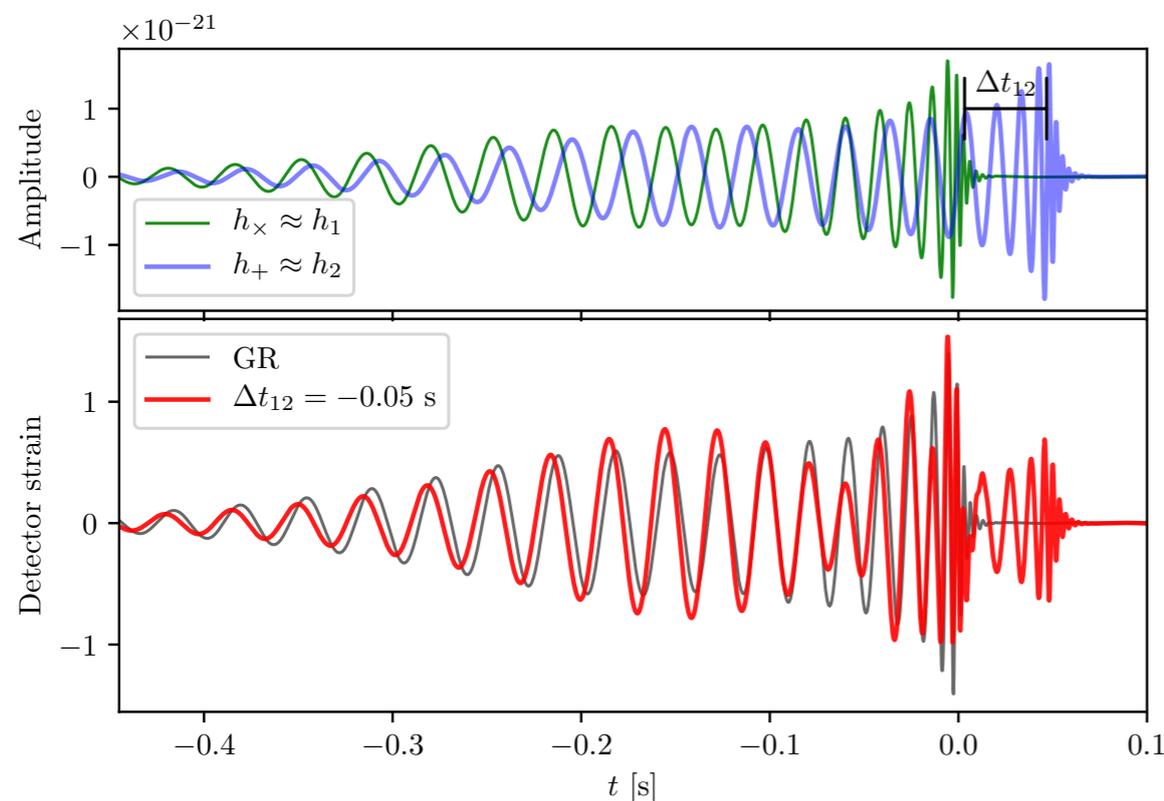
Main effects

Modified effective metric for each eigenstate and polarization mixing

Time delays

Birefringence

- For each lensed image there could be scrambling or echoes
- No need of EM counterpart! Extend cosmological test GW propagation!



Screening in Horndeski

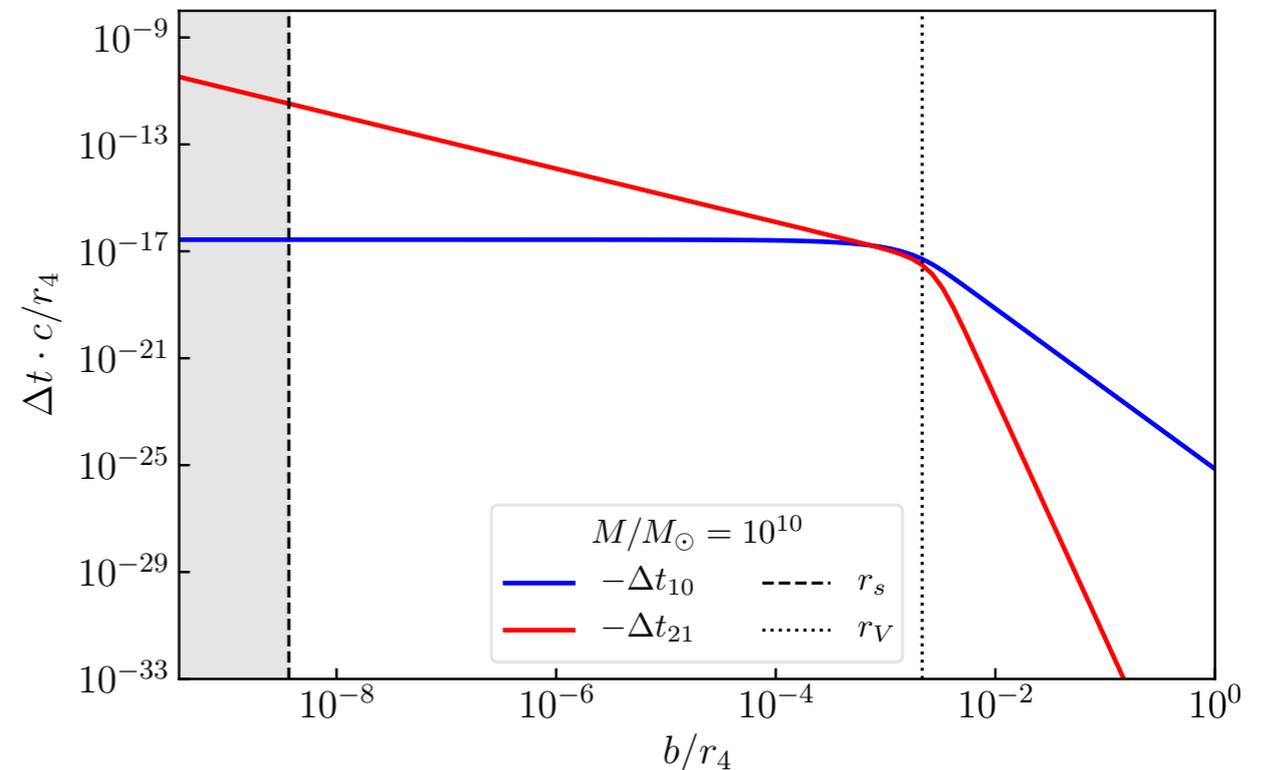
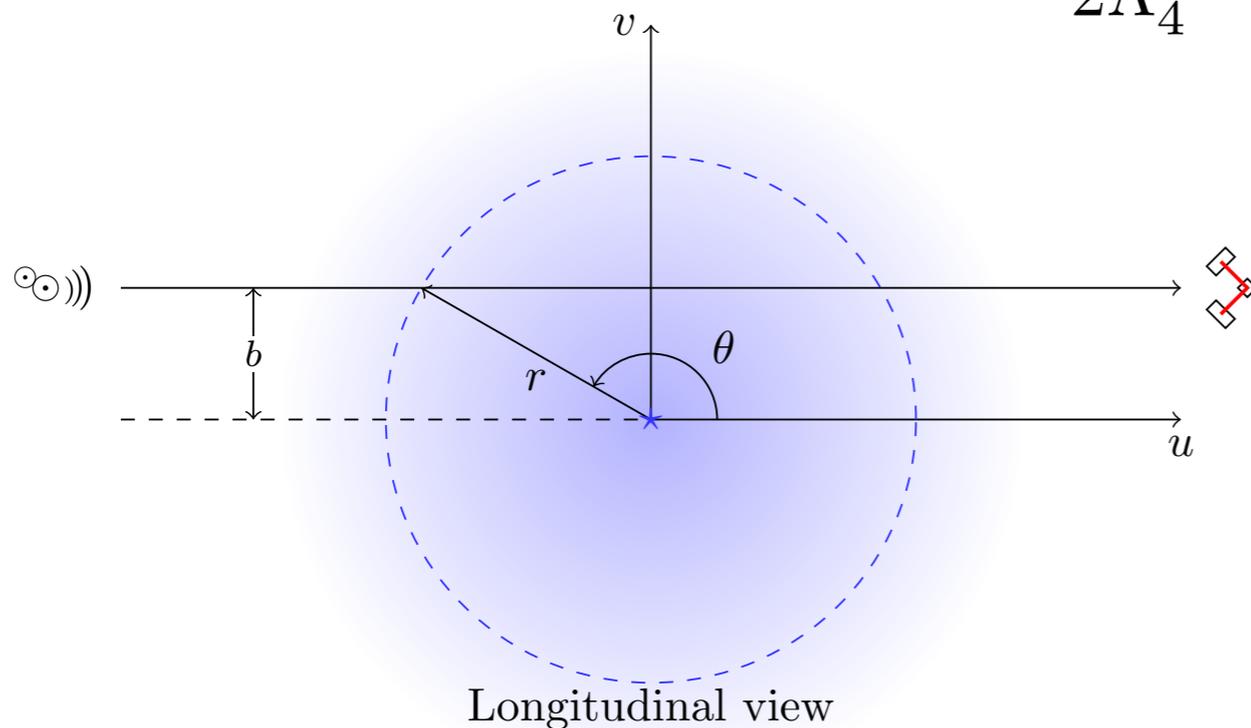
- Let us consider the effect of screening in the GW propagation for a quartic Horndeski theory

$$\mathcal{L} \sim \mathcal{L}_{\text{shift-sym}} + p_{4\phi} \phi M_{\text{Pl}} R \quad G_4 \sim \frac{M_{\text{Pl}}^2}{2} \left(1 + p_{4X} \frac{(\partial\phi)^2}{M_{\text{Pl}}^2 \Lambda_4^2} \right)$$

- Relevant scales: quartic term length scale and Vainshtein radius

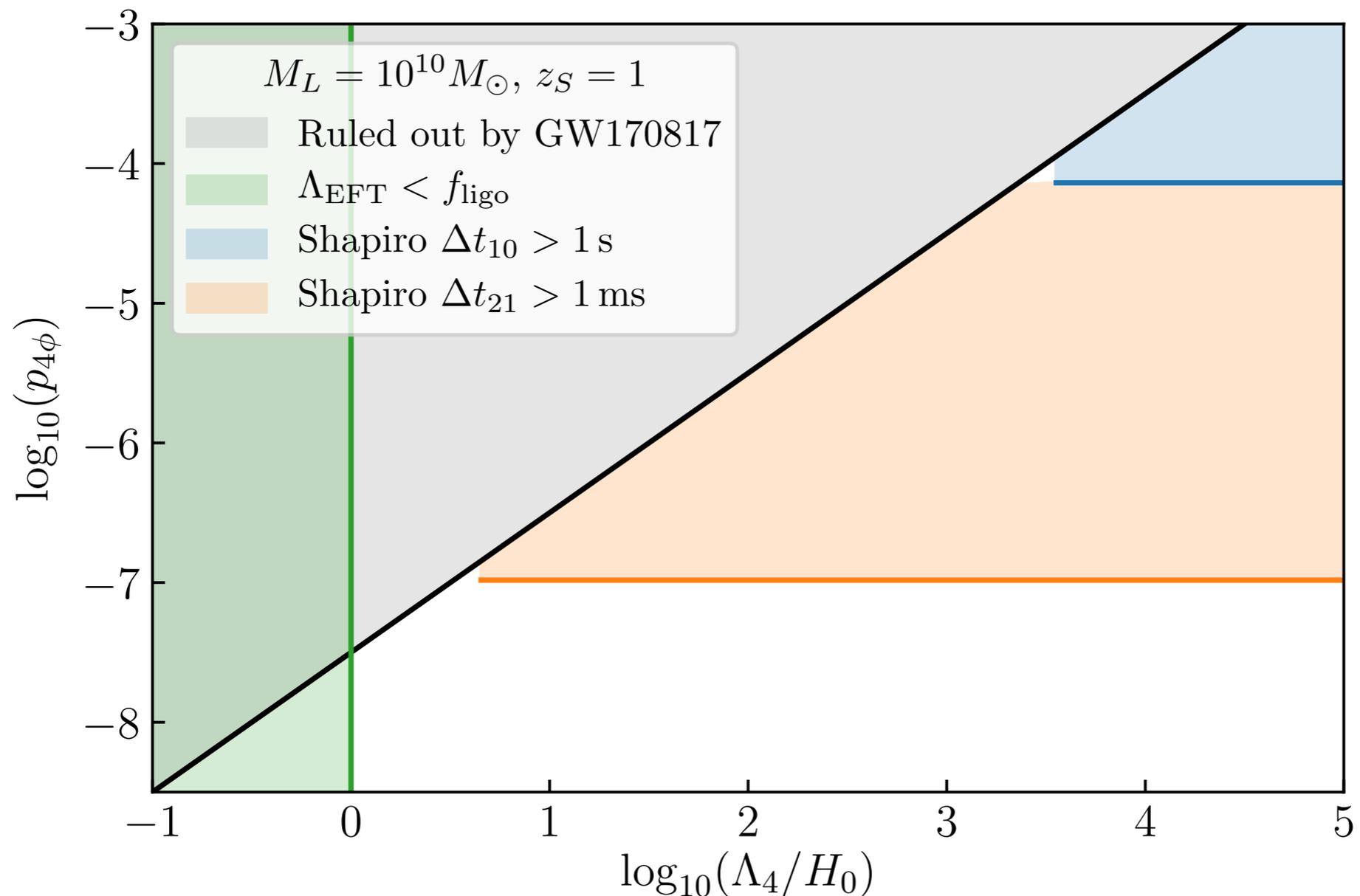
$$(r_4)^3 = \frac{r_s}{2\Lambda_4^2}$$

$$r_V = p_{4\phi}^{1/3} r_4$$



Screening in Horndeski

GW lensing beyond GR **can probe** regions of the parameter space
unconstrained by **GW170817**



LISA cosmology: final thoughts

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We need to anticipate the interesting science in *2034+*

Likely not the same as today, e.g. current H_0 tension

We need to anticipate what LISA will do *uniquely*

Build *synergies*, not repetition

Competition both with EM surveys *and* 3G GW detectors

Many tools can be borrowed from current ground-based GW pipelines

Let's not duplicate efforts and create flexible, public codes!

... but LISA is different

Overlapping signals, high SNR...

Connecting theories modifying emission and propagation...

LISA cosmology: open questions

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