



*Digital quantum computers*  
versus  
*Analog Quantum Simulators*

*Enrique Solano*

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Universidad  
del País Vasco

Euskal Herriko  
Unibertsitatea



**ikerbasque**  
Basque Foundation for Science

*Honouring Peter Zoller by showing some of the works  
in quantum simulation ... I did without him*

*Enrique Solano*

*University of the Basque Country, Bilbao, Spain*

**Solvay Workshop on Quantum Simulations, Brussels, February 2016**



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In this talk, I will share my views on how to **positively** answer to the key question:

*Is it possible to outperform classical computers in the next 10 years?*

**Evidently, any such proposal can only involve:**

- i) few tens of qubits, cavities, motional modes, open transmission lines**
- ii) novel paradigms for quantum computing and quantum simulation**

**Most of my examples will be in circuit QED (cQED) and superconducting circuits (SC)**

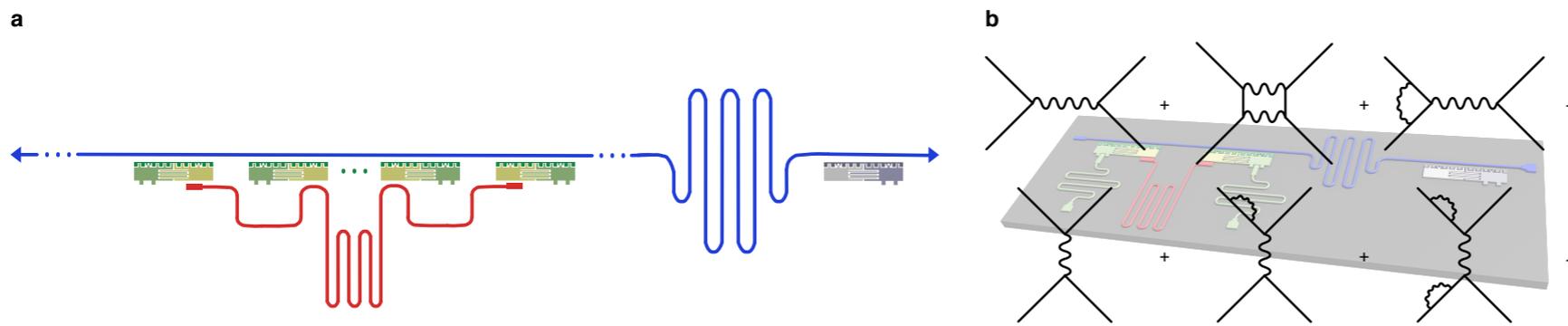


*Bilbao Quantum Machine*

*BQM*

## Quantum field theory models

L. García-Álvarez et al., PRL 2015



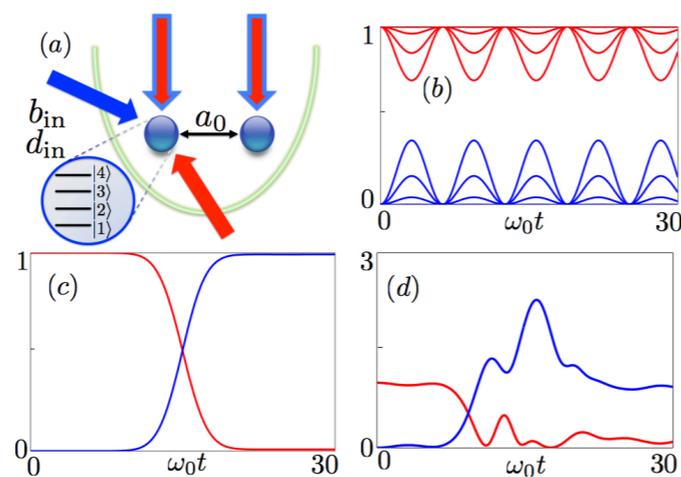
Superconducting circuits

**Complexity  
simulating  
complexity**

**Digital-analog  
quantum simulation**

## Quantum Field Theory models

Casanova et al., PRL 2011



Trapped ions

**Trapped ions require  
discretized field modes**

**cQED naturally enjoys a  
continuum of bosonic modes**

*Bilbao Quantum Machine*

*BQM*



*DQS + AQS + AQC*

*Digital steps provide versatility*

**Digital-Analog  
Quantum Simulation  
DAQS**

*Analog blocks provide complexity*

*Digital steps provide versatility*

**Digital-Adiabatic  
quantum computing  
DAQC**

*Adiabatic blocks provide complexity*

*Embedding Quantum Simulators  
EQS*

**Complexity  
Simulating/Computing  
Complexity**

*Optimal Quantum Control  
OQC*

*Quantum Machine Learning  
QML*

**Neuromorphic  
Quantum Computing  
(NQC)**

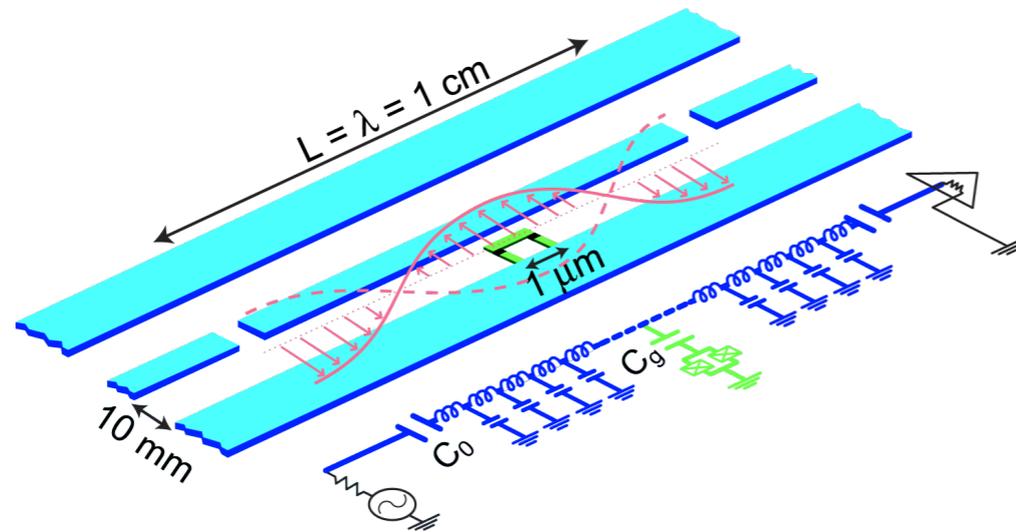
*Quantum Artificial Intelligence  
QAI*

*Quantum memristors provide complexity*

# Circuit QED (cQED) and Superconducting Circuits (SC)

Jaynes-Cummings (JC) model in circuit QED: a field mode represents the field mode, the two-level atom is replaced by a superconducting qubit, also called **artificial atom**.

$$H^T = \omega_r a^\dagger a + \sum_{i=1}^N [4E_{C,i}(n_i - n_{g,i})^2 - E_{J,i} \cos \phi_i + 2\beta_i e V_{\text{rms}} n_i (a + a^\dagger)].$$



*Yale group*

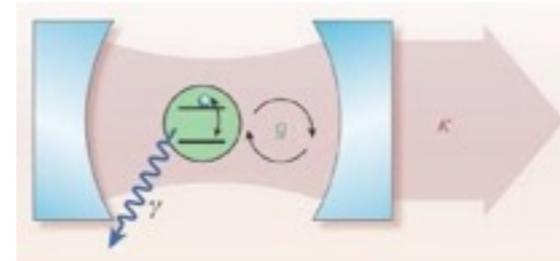
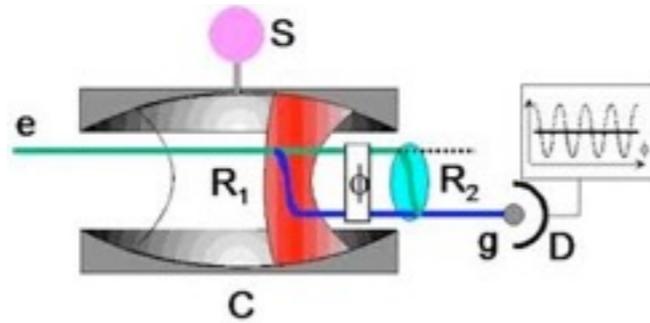
*A. Wallraff et al., Nature 2004*

$$H_{JC} = \frac{\hbar\omega_0}{2} \sigma_z + \hbar\omega a^\dagger a + \hbar g (\sigma^+ a + \sigma^- a^\dagger)$$

It is an unacknowledged **quantum simulation** of the JC model in circuit QED.

# Two motivations for quantum simulations

I) Quantum simulation establishes analogies between unconnected fields, it is a communication vessel producing a flood of knowledge in both directions.

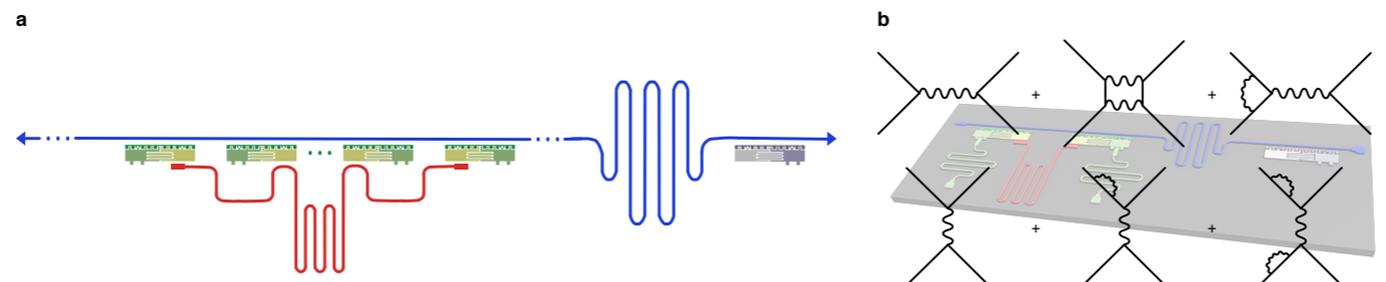


cQED has advantages in atomic control that overcomes those of microwave CQED, and, at the same time, it enjoys longitudinal and transversal driving as in optical CQED.

**MANTRA: the same model in another quantum platform always brings novel physics: strongly dispersive regime, USC & DSC of light-matter in cavities and open TLs, etc.**

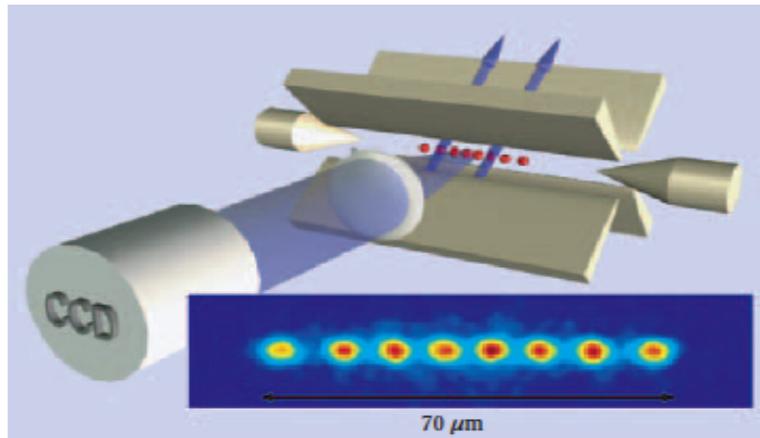
II) Quantum simulations will allow us to predict and explain novel physics when we will be able to implement scalable quantum simulators.

For instance, solving complex problems in condensed matter, quantum chemistry, quantum field theory, machine learning, and artificial intelligence.



# Which was the first quantum simulation experiment?

We could consider the implementation of the **JC model in trapped ions** as (one of) the first nontrivial **quantum simulations**.



$$H_0 = \hbar\nu\left(a^\dagger a + \frac{1}{2}\right)$$

$$H_r = \hbar\eta\tilde{\Omega}_r\left(\sigma^+ a e^{i\phi_r} + \sigma^- a^\dagger e^{-i\phi_r}\right)$$

Red sideband excitation of the ion = JC interaction

$$H_b = \hbar\eta\tilde{\Omega}_b\left(\sigma^+ a^\dagger e^{i\phi_b} + \sigma^- a e^{-i\phi_b}\right)$$

Blue sideband excitation of the ion = anti-JC interaction

The quantized electromagnetic field is replaced by quantized ion motion

*This allowed Cirac & Zoller to propose in 1995 the first implementable two-qubit gate for universal QC in trapped ions!*

**MANTRA:** *the same model in another quantum platform always brings novel physics, ... if you are creative enough.*

*Bilbao Quantum Machine*

*BQM*



*DQS + AQS + AQC*

*Digital steps provide versatility*

**Digital-Analog  
Quantum Simulation  
DAQS**

*Analog blocks provide complexity*

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**Digital-Adiabatic  
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(NQC)**

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*Quantum memristors provide complexity*

# *Digital quantum machines*

There are two classes of digital quantum machines:

- 1) Digital (gate-based) quantum computer (DQC)*
- 2) Digital quantum simulator (DQS)*

A DQC can become universal, fault tolerant, and scalable.

It is meant to perform general-purpose quantum algorithms (e.g., Grover & Shor).

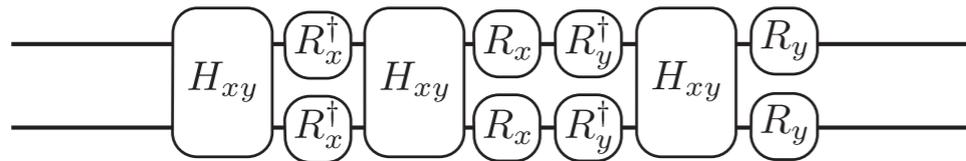
A DQS is not meant to be universal, but it could turn fault tolerant and scalable.

It is essentially a purpose-oriented DQC that mimics models (spins, bosons, fermions).

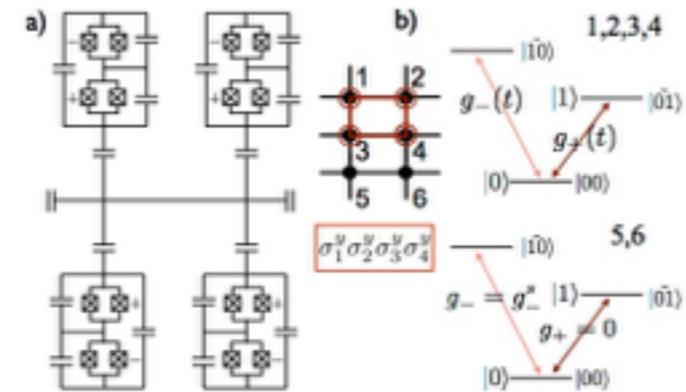
*DQC/DQS may not be able to outperform classical computers with prethreshold quantum platforms, and fault-tolerant approaches demand millions of gates/qubits.*

# DQS with superconducting circuits: Bilbao theory

**DQS of spin Models with SC**  
*Las Heras et al., PRL 2014*

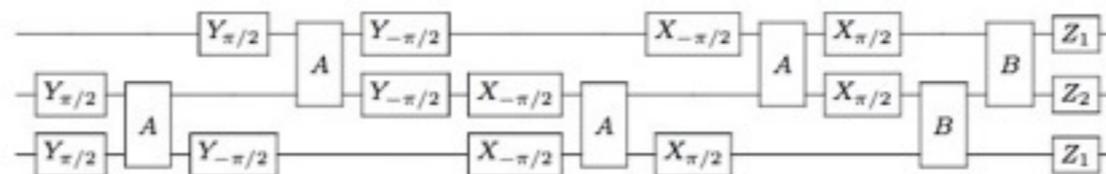


**Multiqubit gates & MS gates with SC**  
*Mezzacapo et al. PRL 2014*



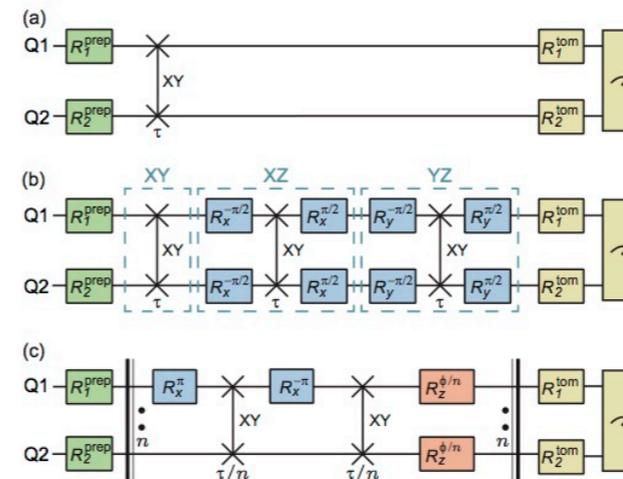
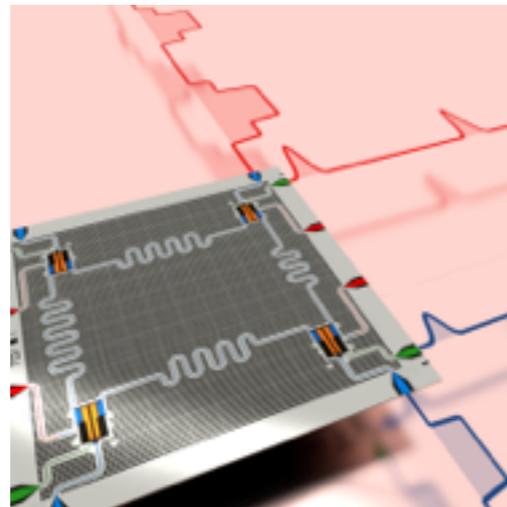
**DQS of fermionic models with SC**  
*Las Heras et al., EPJ QT 2015*

Table 1 Sequence of gates for one Trotter step of Hamiltonian 2.



# First DQS of spin models with superconducting circuits

## Collaboration Bilbao-Zürich



PHYSICAL REVIEW X **5**, 021027 (2015)

### Digital Quantum Simulation of Spin Models with Circuit Quantum Electrodynamics

Y. Salathé,<sup>1,\*</sup> M. Mondal,<sup>1</sup> M. Oppliger,<sup>1</sup> J. Heinsoo,<sup>1</sup> P. Kurpiers,<sup>1</sup> A. Potočnik,<sup>1</sup> A. Mezzacapo,<sup>2</sup>  
U. Las Heras,<sup>2</sup> L. Lamata,<sup>2,3</sup> E. Solano,<sup>2,3</sup> S. Filipp,<sup>1,†</sup> and A. Wallraff<sup>1</sup>

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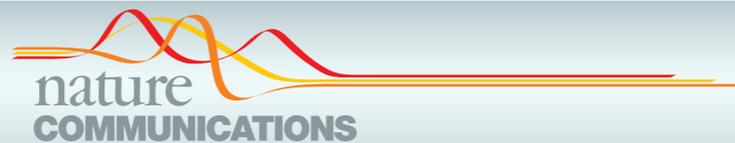
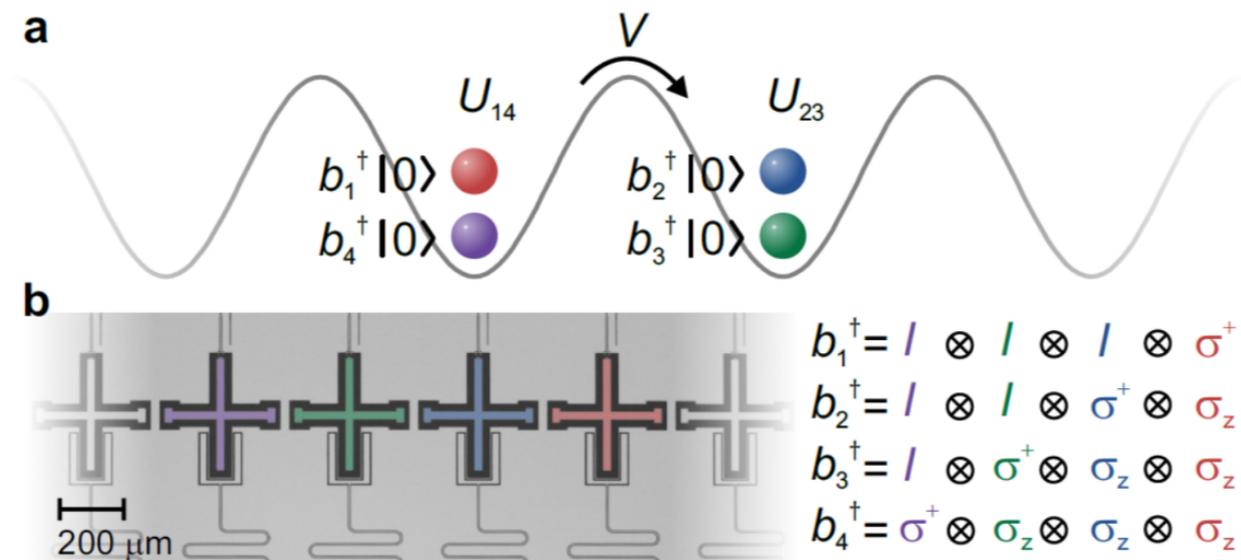
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(Received 6 March 2015; published 17 June 2015)

# DQS with superconducting circuits: experiments

First DQS of fermionic models with superconducting circuits

Collaboration Bilbao-Google (UCSB)



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OPEN

## Digital quantum simulation of fermionic models with a superconducting circuit

R. Barends<sup>1</sup>, L. Lamata<sup>2</sup>, J. Kelly<sup>3,†</sup>, L. García-Álvarez<sup>2</sup>, A.G. Fowler<sup>1</sup>, A. Megrant<sup>3,4</sup>, E. Jeffrey<sup>1</sup>, T.C. White<sup>3</sup>, D. Sank<sup>1</sup>, J.Y. Mutus<sup>1</sup>, B. Campbell<sup>3</sup>, Yu Chen<sup>1</sup>, Z. Chen<sup>3</sup>, B. Chiaro<sup>3</sup>, A. Dunsworth<sup>3</sup>, I.-C. Hoi<sup>3</sup>, C. Neill<sup>3</sup>, P.J.J. O'Malley<sup>3</sup>, C. Quintana<sup>3</sup>, P. Roushan<sup>1</sup>, A. Vainsencher<sup>3</sup>, J. Wenner<sup>3</sup>, E. Solano<sup>2,5</sup> & John M. Martinis<sup>1,3</sup>

*First digitization of adiabatic quantum computing  
with superconducting circuits*

***Collaboration Bilbao-Google (UCSB & LA)***

**Digitized adiabatic quantum computing with a superconducting circuit**

R. Barends,<sup>1</sup> A. Shabani,<sup>2</sup> L. Lamata,<sup>3</sup> J. Kelly,<sup>1</sup> A. Mezzacapo,<sup>3,\*</sup> U. Las Heras,<sup>3</sup> R. Babbush,<sup>2</sup> A. G. Fowler,<sup>1</sup> B. Campbell,<sup>4</sup> Yu Chen,<sup>1</sup> Z. Chen,<sup>4</sup> B. Chiaro,<sup>4</sup> A. Dunsworth,<sup>4</sup> E. Jeffrey,<sup>1</sup> E. Lucero,<sup>1</sup> A. Megrant,<sup>4</sup> J. Y. Mutus,<sup>1</sup> M. Neeley,<sup>1</sup> C. Neill,<sup>4</sup> P. J. J. O'Malley,<sup>4</sup> C. Quintana,<sup>4</sup> P. Roushan,<sup>1</sup> D. Sank,<sup>1</sup> A. Vainsencher,<sup>4</sup> J. Wenner,<sup>4</sup> T. C. White,<sup>4</sup> E. Solano,<sup>3,5</sup> H. Neven,<sup>2</sup> and John M. Martinis<sup>1,4</sup>

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<sup>5</sup>*IKERBASQUE, Basque Foundation for Science, Maria Diaz de Haro 3, 48013 Bilbao, Spain.*

A major challenge in quantum computing is to solve general problems with limited physical hardware. Here, we implement digitized adiabatic quantum computing, combining the generality of the adiabatic algorithm with the universality of the digital approach, using a superconducting circuit with nine qubits. We probe the adiabatic evolutions, and quantify the success of the algorithm for random spin problems. We find that the system can approximate the solutions to both frustrated Ising problems and problems with more complex interactions, with a performance that is comparable. The presented approach is compatible with small-scale systems as well as future error-corrected quantum computers.

*R. Barends et al., arXiv:1511.03316*

## *Analog quantum machines*

There are two classes of analog quantum machines:

*1) Analog quantum simulator (AQS)*

*2) Analog quantum computer (AQC)*

An AQS is not meant to be universal but it could, in principle, outperform classical computers. Optical lattices and quantum photonics are trying hard. Trapped ions and SC should also bet.

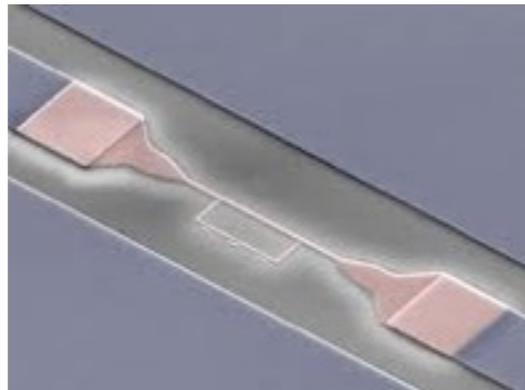
An AQC can be represented by adiabatic quantum computing or quantum annealing. It performs quantum computations by encoding classes of optimization problems.

*AQS/AQC may not outperform classical devices with prethreshold quantum platforms. It is usually accepted without demonstration that AQS/AQC cannot become fault tolerant.*

## *Ultrastrong coupling (USC) regime of the quantum Rabi model*

We have recently seen the advent of the **ultrastrong coupling (USC)** regime of light-matter interactions **in cQED**, where  $0.1 < g/w < 1$ , and **RWA cannot be applied**.

$$H_{QRM} = \frac{\hbar\omega_0}{2}\sigma_z + \hbar\omega a^\dagger a + \hbar g(\sigma^+ + \sigma^-)(a^\dagger + a)$$



T. Niemczyk et al., Nature Phys. **6**, 772 (2010)

P. Forn-Díaz et al., PRL **105**, 237001 (2010)

Recently, the analytical solutions of the QRM were presented: D. Braak, PRL **107**, 100401 (2011).

Current experimental efforts are trying to approach nonperturbative USC regimes, where  $g/w \sim 0.5-1.0$

Very recent works, see arXiv and APS March Meeting abstracts, announce even the experimental arrival of the deep strong coupling (DSC) regime of light-matter interactions.

The DSC regime was proposed and studied in Casanova et al., PRL 2010

# Deep strong coupling (DSC) regime of the QRM

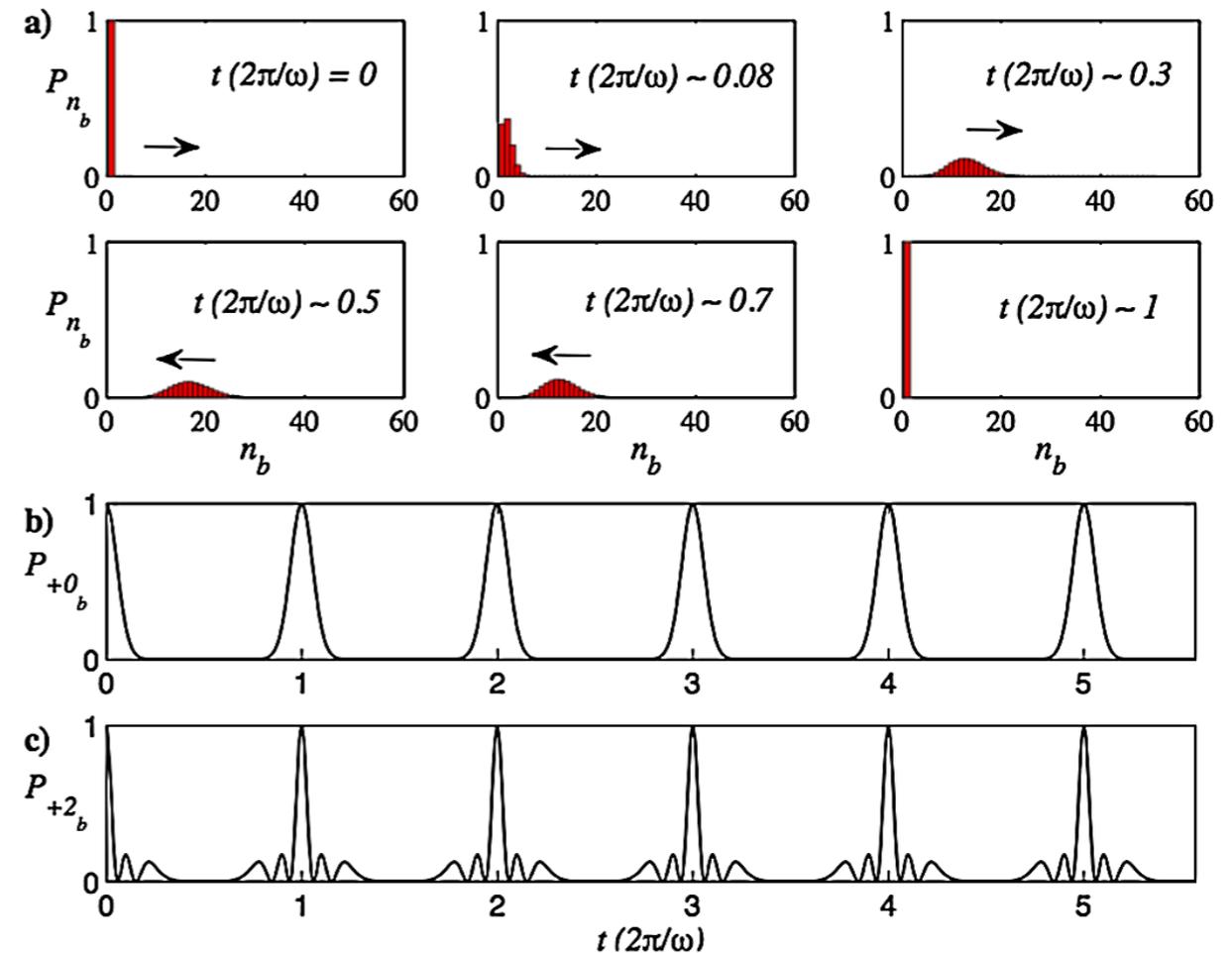
The DSC regime of the JC model happens when  $g/w > 1.0$ , and it has been questioned whether such a regime could be experimentally reached or ever exist in nature.

$$\Pi = -\sigma_z(-1)^{n_a} = -(|e\rangle\langle e| - |g\rangle\langle g|)(-1)^{a^\dagger a}$$

$$|g0_a\rangle \leftrightarrow |e1_a\rangle \leftrightarrow |g2_a\rangle \leftrightarrow |e3_a\rangle \leftrightarrow \dots (p = +1)$$

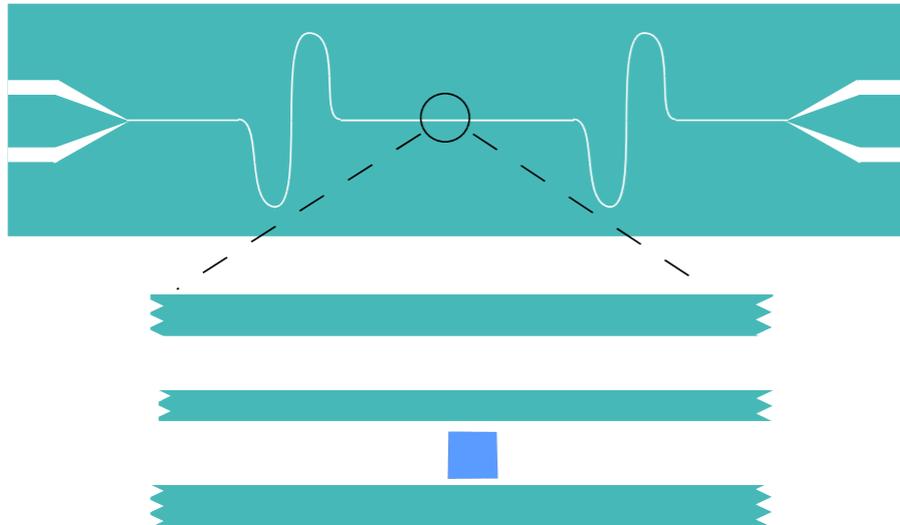
$$|e0_a\rangle \leftrightarrow |g1_a\rangle \leftrightarrow |e2_a\rangle \leftrightarrow |g3_a\rangle \leftrightarrow \dots (p = -1)$$

Forget about Rabi oscillations or perturbation theory:  
 parity chains and photon number wavepackets  
 define the physics of the DSC regime.



# *AQS with superconducting circuits: Bilbao theory*

## *AQS of USC & DSC regimes of the quantum Rabi model*



$$\mathcal{H}_{\text{JC}} = \frac{\hbar\omega_q}{2}\sigma_z + \hbar\omega a^\dagger a + \hbar g(\sigma^\dagger a + \sigma a^\dagger)$$

Two-tone microwave driving

$$\mathcal{H}_D = \hbar\Omega_1(e^{i\omega_1 t}\sigma + \text{H.c.}) + \hbar\Omega_2(e^{i\omega_2 t}\sigma + \text{H.c.})$$

Leads to the effective Hamiltonian: QRM in all regimes

$$\mathcal{H} = \hbar(\omega - \omega_1)a^\dagger a + \frac{\hbar\Omega_2}{2}\sigma_z + \frac{\hbar g}{2}\sigma_x(a + a^\dagger)$$

A two-tone driving in cavity QED or circuit QED can turn any JC model into a USC or DSC regime of the QRM model.

# *Digital quantum machines or analog quantum machines?*

Digital quantum machines and analog quantum machines have polarized SS and AMO communities. Where is your place in this debate?

**This debate is flawed or may not exist at all.**

We propose

**digital-analog quantum simulation (DAQS)**

with prethreshold quantum devices to outperform classical computers in the next 10 years.

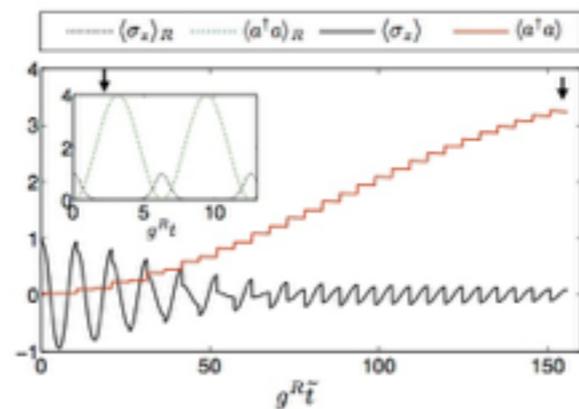
# Complexity Simulating Complexity

*A first experiment in DAQS for superconducting circuits*

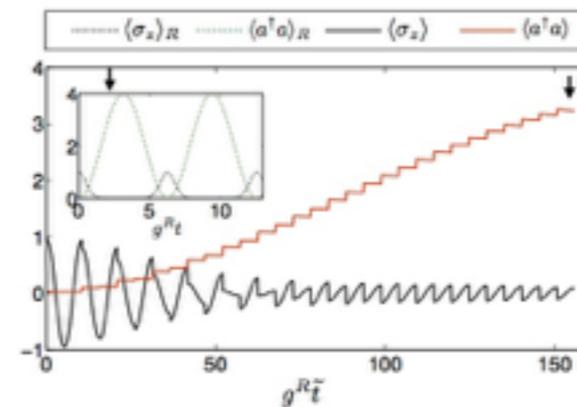
***Bilbao theory + Delft experiment?***

**Digital quantum Rabi and Dicke models**

*Mezzacapo et al., Sci. Rep. 2014*



**Experiment at TU Delft?**



In DAQS, **analog blocks** are combined sequentially with **digital steps**.

**Analog blocks** are made of collective quantum gates, that is, in-built complex operations.

**Digital steps** are local quantum operations that may act also in a global manner.

**Analog blocks provide the complexity** of the simulated model, **digital steps provide flexibility**.

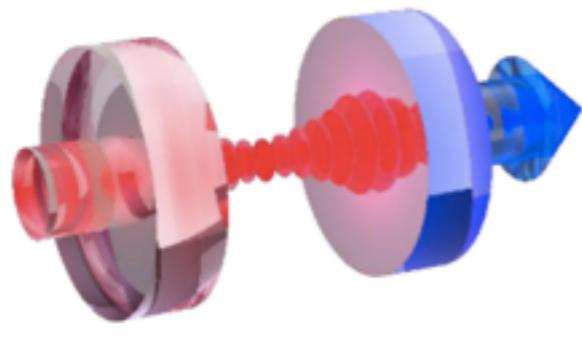
Similar spirit can be followed by introducing digital-adiabatic quantum computers (DAQC).

# *How DAQS works on superconducting circuits?*

## Digital quantum Rabi and Dicke models

*Mezzacapo et al., Sci. Rep. 2014*

Quantum Rabi model: most fundamental light-matter interaction



$$H_R = \omega_r^R a^\dagger a + \frac{\omega_q^R}{2} \sigma^z + g^R \sigma^x (a^\dagger + a)$$

Small coupling as compared to mode & qubit frequencies: Jaynes-Cummings model

$$H = \omega_r a^\dagger a + \frac{\omega_q}{2} \sigma^z + g(a^\dagger \sigma^- + a \sigma^+)$$

## Digital quantum Rabi and Dicke models

*Mezzacapo et al., Sci. Rep. 2014*

Interaction available in cQED: Jaynes-Cummings model

$$H = \omega_r a^\dagger a + \frac{\omega_q}{2} \sigma^z + g(a^\dagger \sigma^- + a \sigma^+)$$



Digital decomposition: JC + local rotations

$$H_R = H_1 + H_2, \quad \begin{aligned} H_1 &= \frac{\omega_r^R}{2} a^\dagger a + \frac{\omega_q^1}{2} \sigma^z + g(a^\dagger \sigma^- + a \sigma^+), \\ H_2 &= \frac{\omega_r^R}{2} a^\dagger a - \frac{\omega_q^2}{2} \sigma^z + g(a^\dagger \sigma^+ + a \sigma^-), \end{aligned}$$

## Digital quantum Rabi and Dicke models

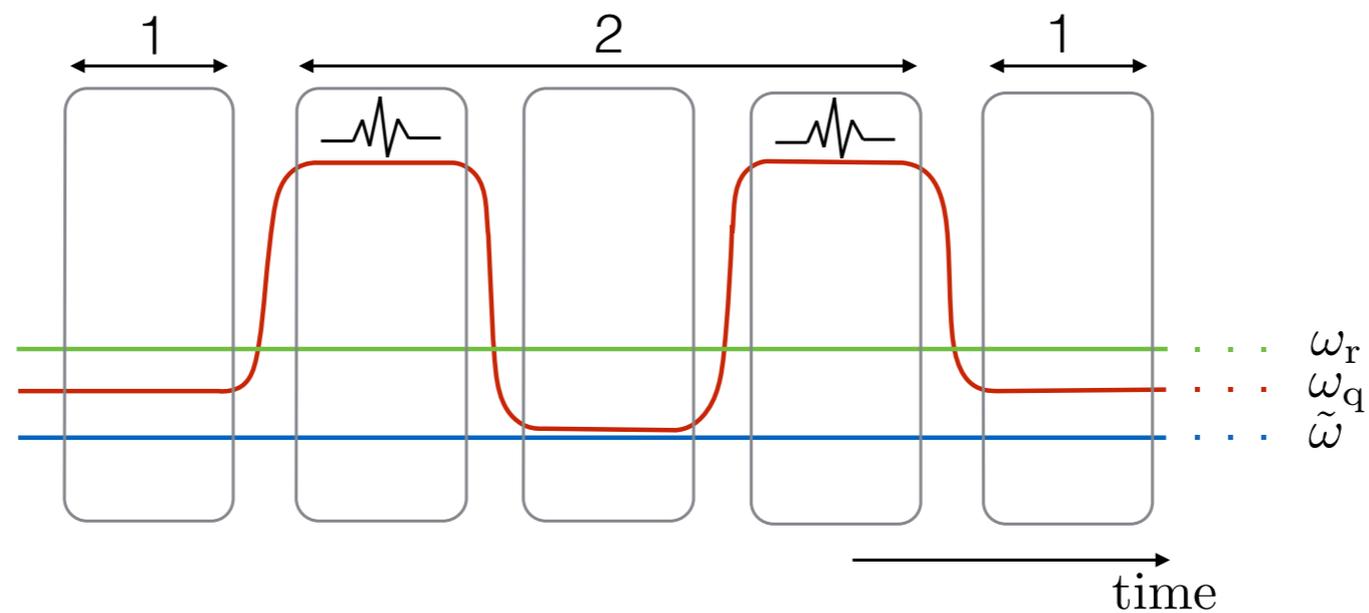
*Mezzacapo et al., Sci. Rep. 2014*

JC in interaction picture  $\tilde{H} = \tilde{\Delta}_r a^\dagger a + \tilde{\Delta}_q \sigma^z + g(a^\dagger \sigma^- + a \sigma^+),$

and we get AJC  $e^{-i\pi\sigma^x/2} \tilde{H} e^{i\pi\sigma^x/2} = \tilde{\Delta}_r a^\dagger a - \tilde{\Delta}_q \sigma^z + g(a^\dagger \sigma^+ + a \sigma^-).$



Trotterization

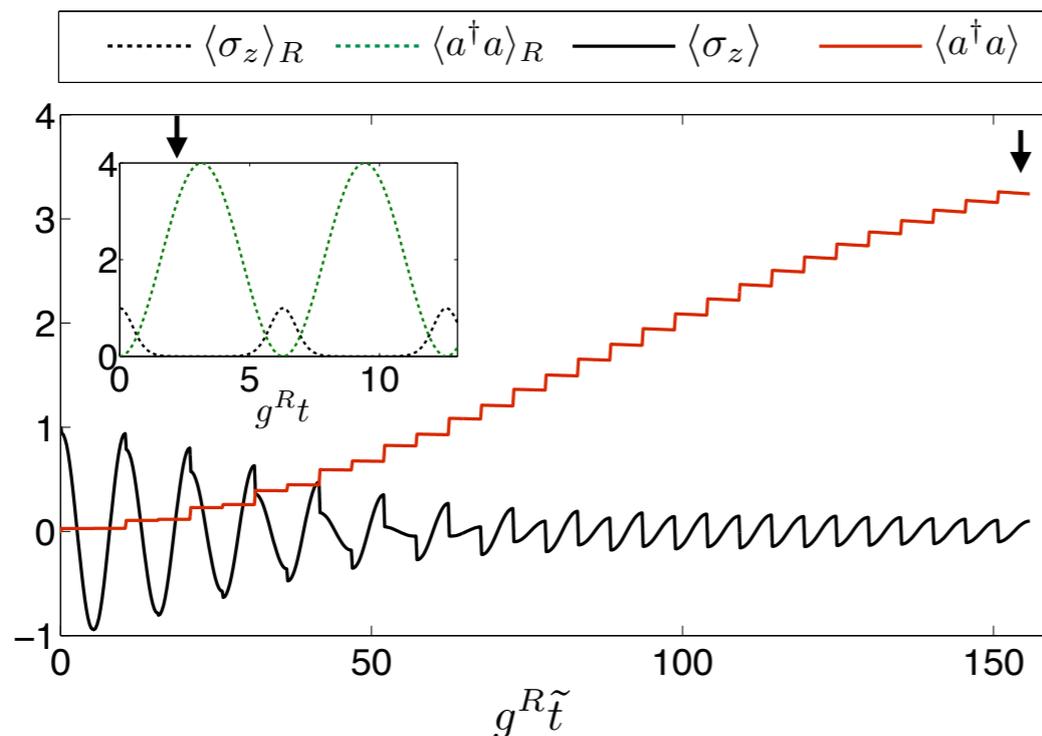


## Digital quantum Rabi and Dicke models

*Mezzacapo et al., Sci. Rep. 2014*

$g^R = \omega_q^R / 2 = \omega_r^R / 2$	$\tilde{\omega} = 7.4 \text{ GHz}, \omega_q^1 - \omega_q^2 = 200 \text{ MHz}$
$g^R = \omega_q^R = \omega_r^R$	$\tilde{\omega} = 7.45 \text{ GHz}, \omega_q^1 - \omega_q^2 = 100 \text{ MHz}$
$g^R = 2\omega_q^R = \omega_r^R$	$\tilde{\omega} = 7.475 \text{ GHz}, \omega_q^1 - \omega_q^2 = 100 \text{ MHz}$

Some parameters...

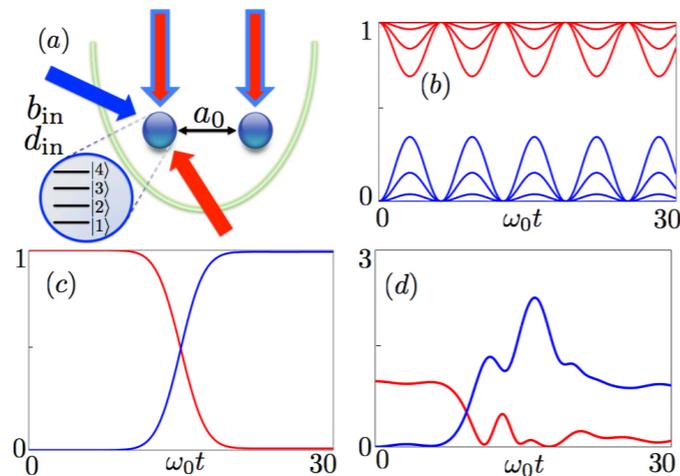


$$\omega_q^R = 0, \text{ and } g^R = \omega_r^R.$$

**USC & DSC regimes are simulated. Move now towards to the Dicke model!**

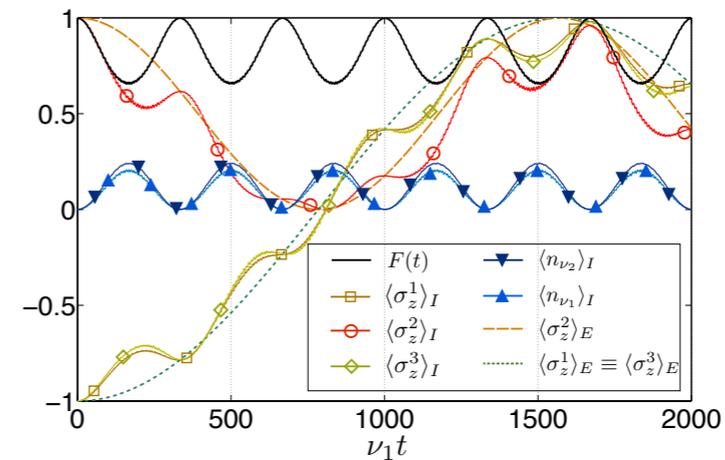
# Further works involving DAQS concepts

**Quantum Field Theory models**  
Casanova et al., PRL 2011



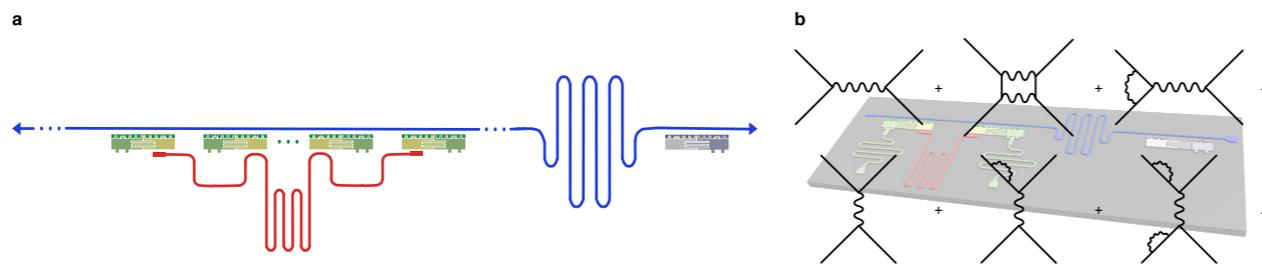
Trapped ions

**Holstein Models**  
Mezzacapo et al., PRL 2012



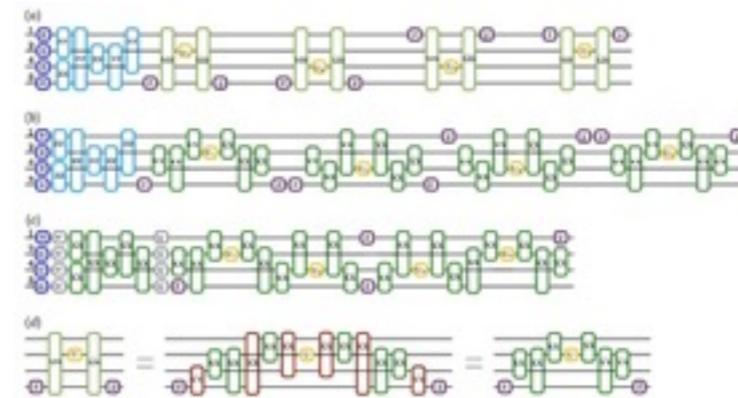
Trapped ions

**Quantum field theory models**  
L. García-Álvarez et al., PRL 2015



Superconducting circuits

**Quantum chemistry models**  
L. García-Álvarez et al., arXiv 2015



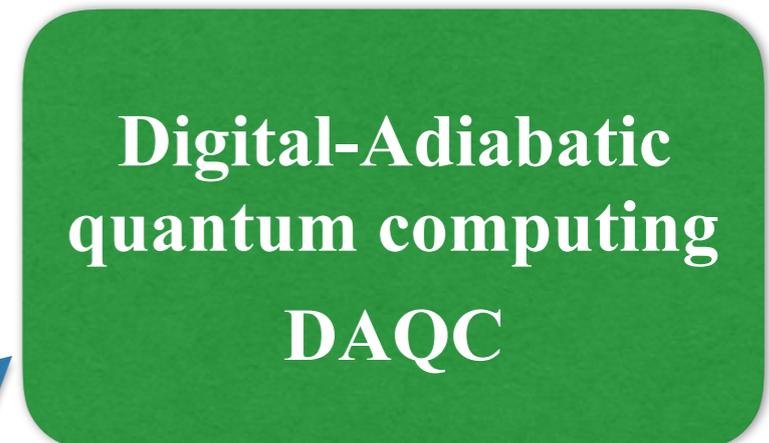
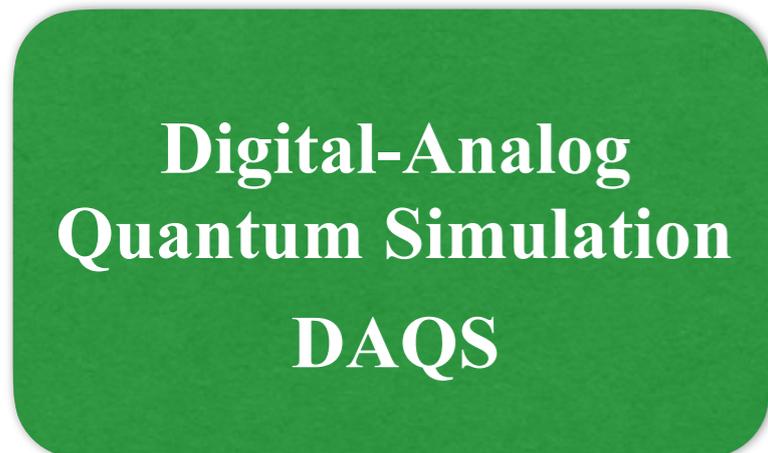
Superconducting circuits

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*Quantum memristors provide complexity*